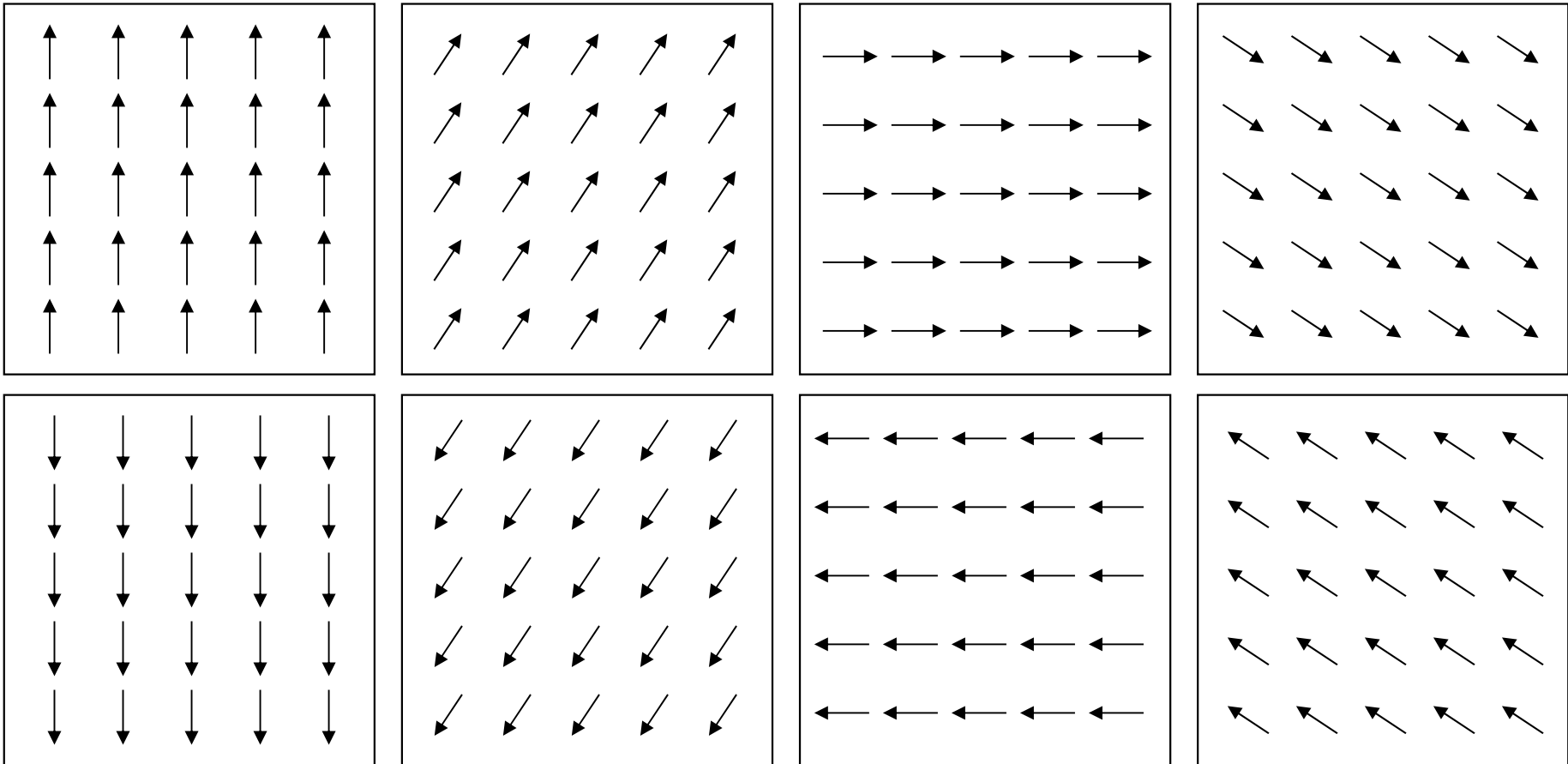


Anisotropía magnetocristalina

Sólo intercambio
(ausencia de anisotropía)

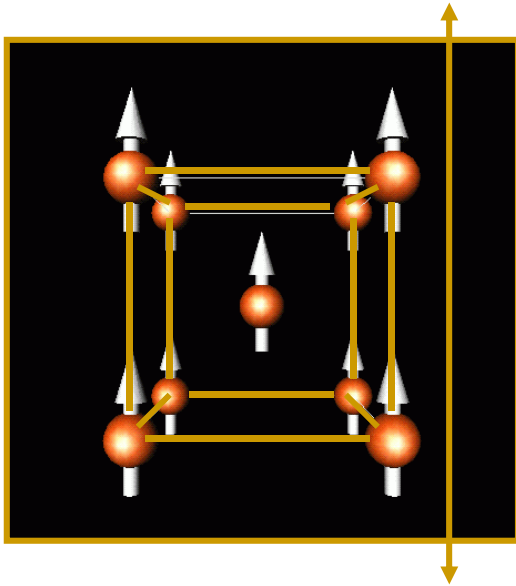
Dirección aleatoria de \mathbf{M} en $4\pi \Rightarrow$ estado continuamente degenerado



Siempre estaríamos en presencia de un superparamagneto

Anisotropía

Fe



Estructura cristalina



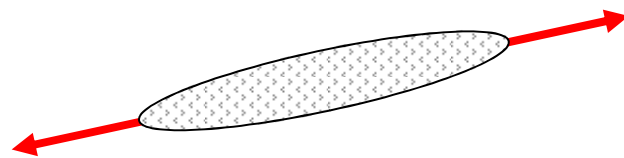
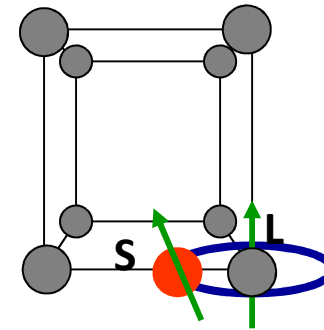
Int. elect - Campo cristalino

+

interacción Spin - órbita

=

Anisotropía magneto-cristalina

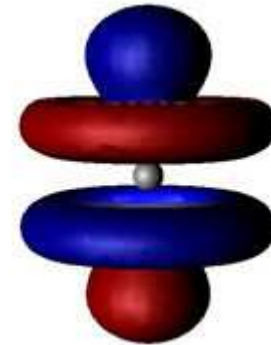
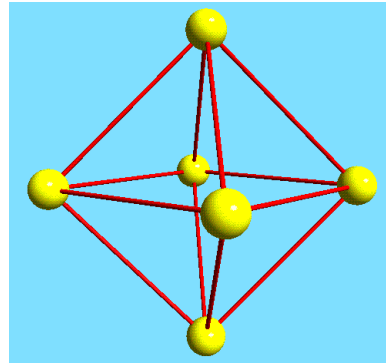
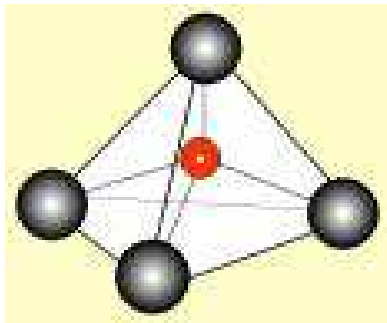
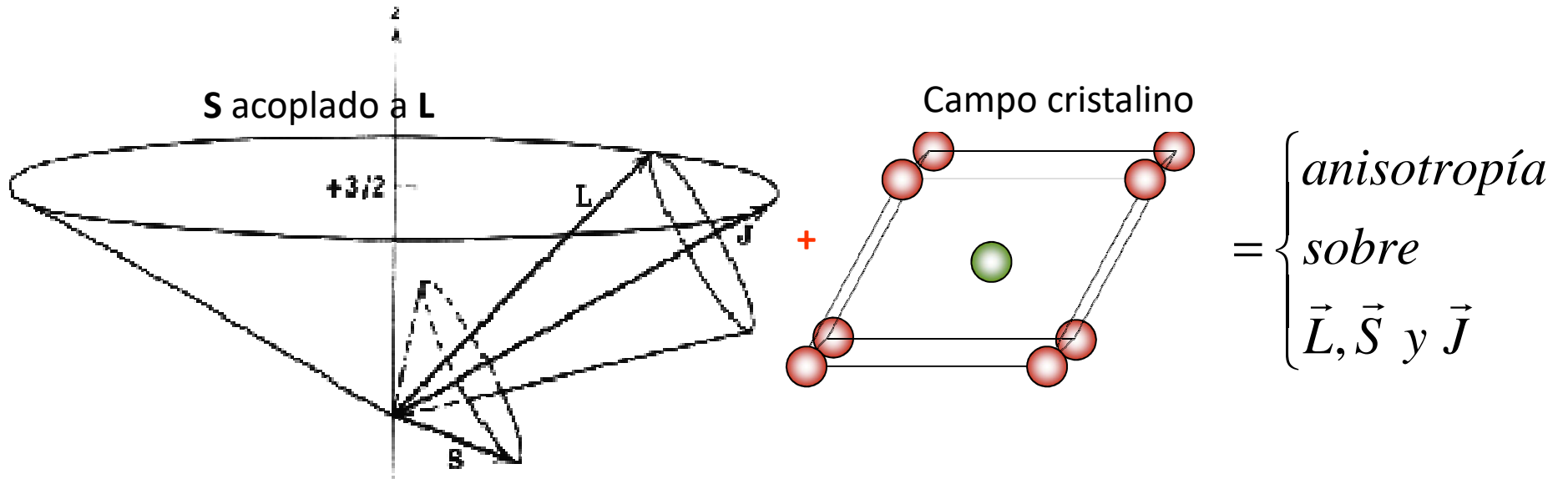


Forma: anisotropía magnetostática



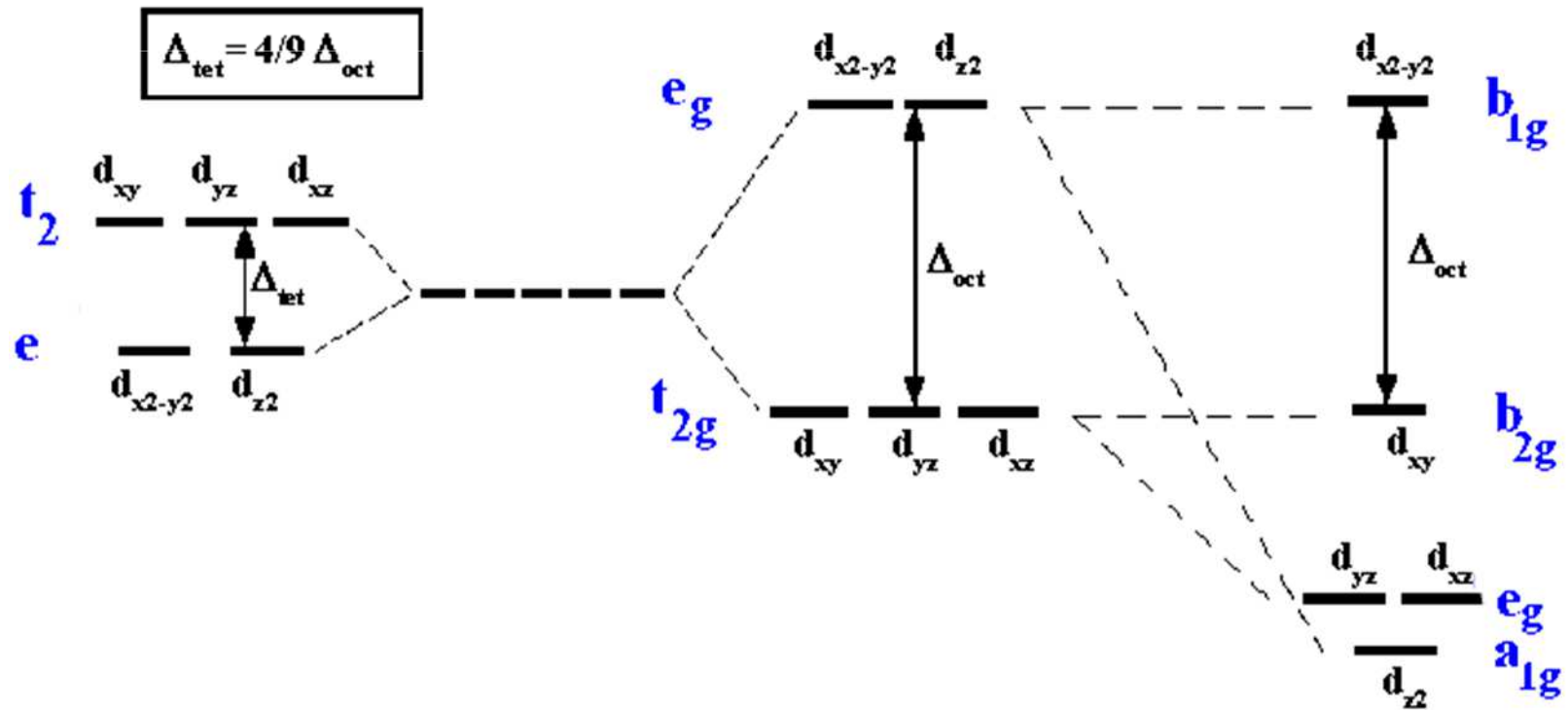
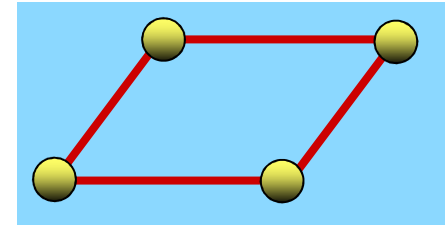
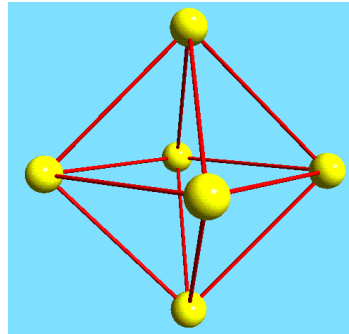
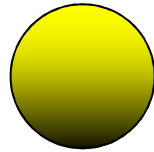
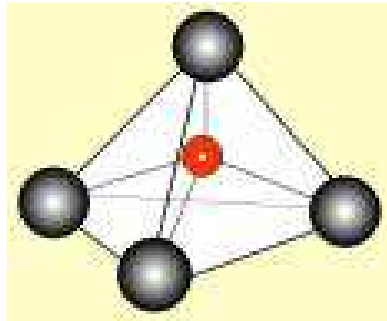
Esfuerzo: anisotropía magnetoelástica

spin – órbita + campo cristalino



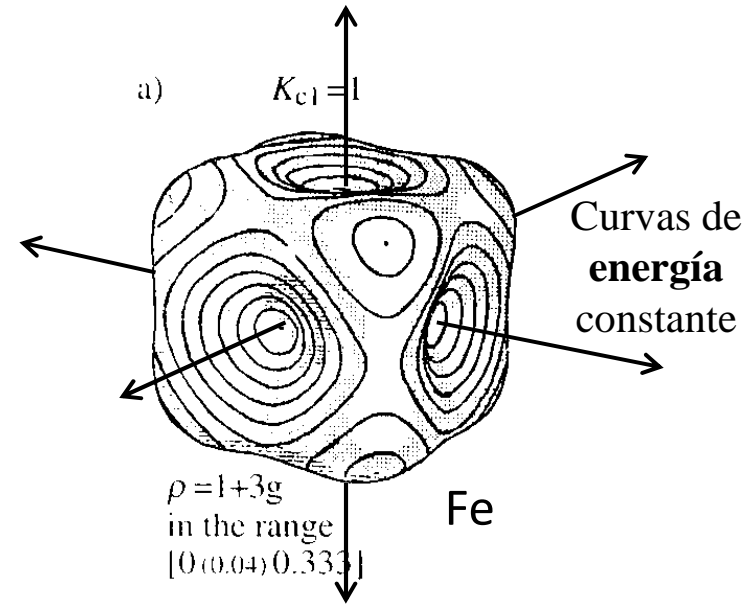
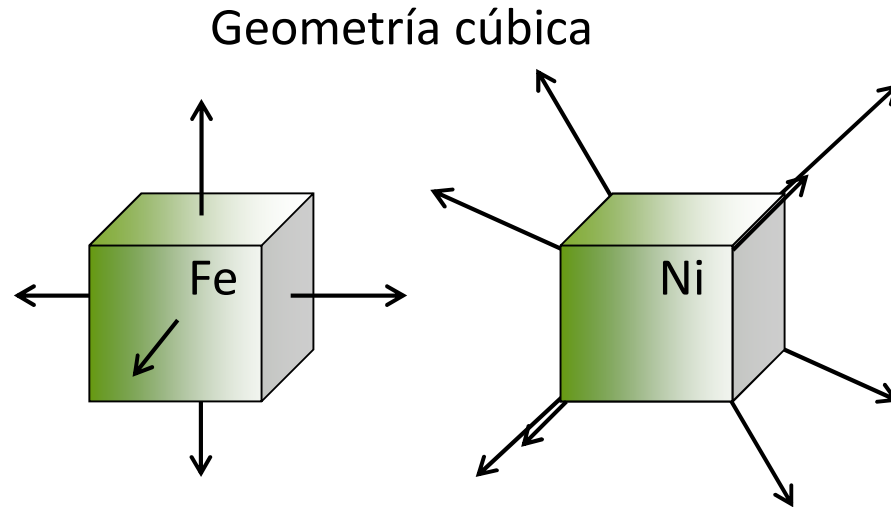
Diagramas de desdoblamiento de orbitales d por el campo cristalino

Campo tetraédrico ión libre campo octaédrico campo planar cuadrado

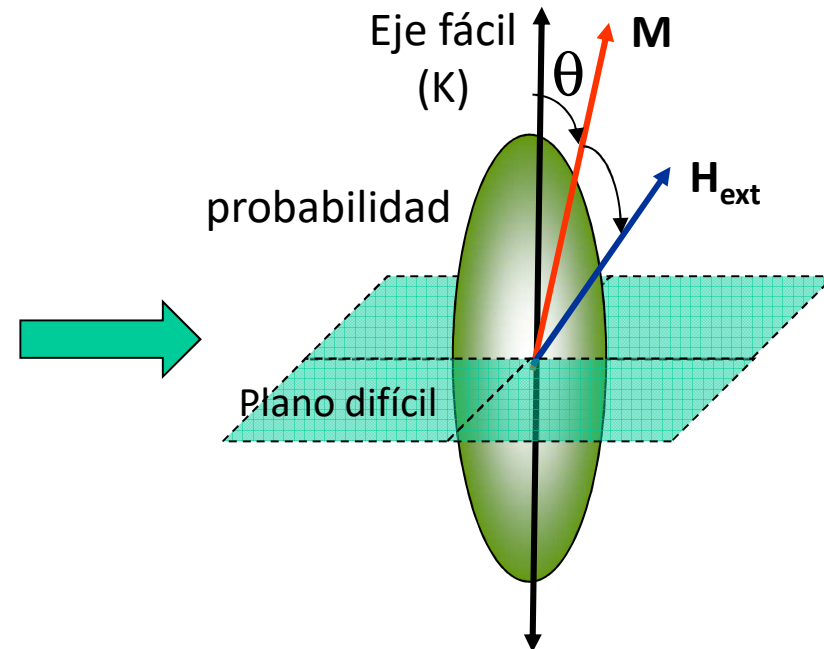
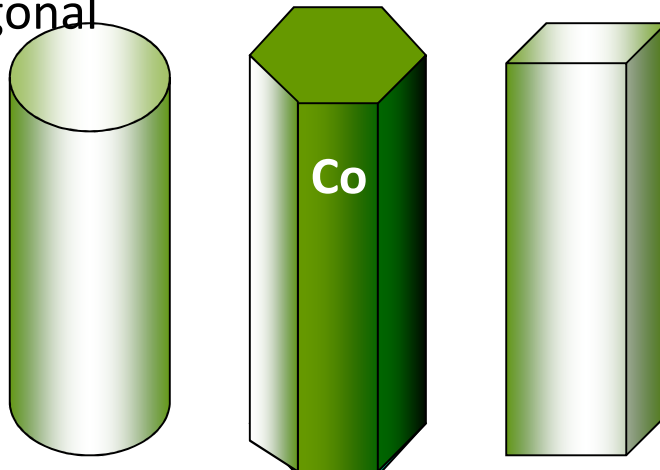


Energía de anisotropía Magnetocristalina

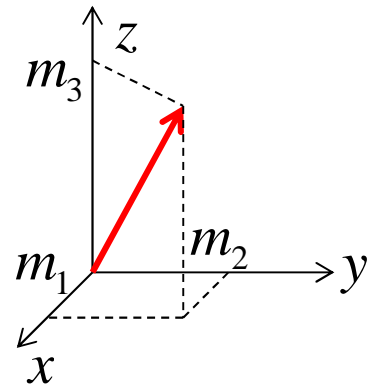
Definiciones



Geometría cilíndrica, tetragonal, hexagonal



Anisotropía – descripción fenomenológica



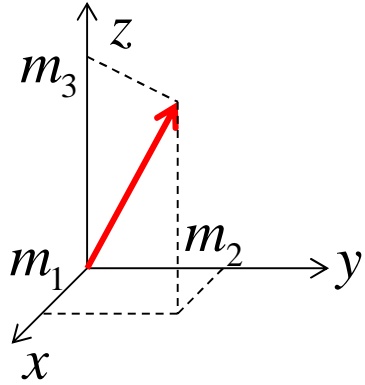
m_i cosenos directores de la magnetización

$$m_{1,2,3} = \frac{M_{x,y,z}}{M} \dots = \cos(\theta_{1,2,3})$$

e_K energía de anisotropía por unidad de volumen

$$e_K = \sum_i K_i m_i^2 + \sum_{ij} K_{ij} m_i^2 m_j^2 + K_{123} m_1^2 m_2^2 m_3^2 + \sum_{ij} K'_{ij} m_i^4 m_j^4 + \dots$$

E_K energía de anisotropía $E_K = \int e_K dV$



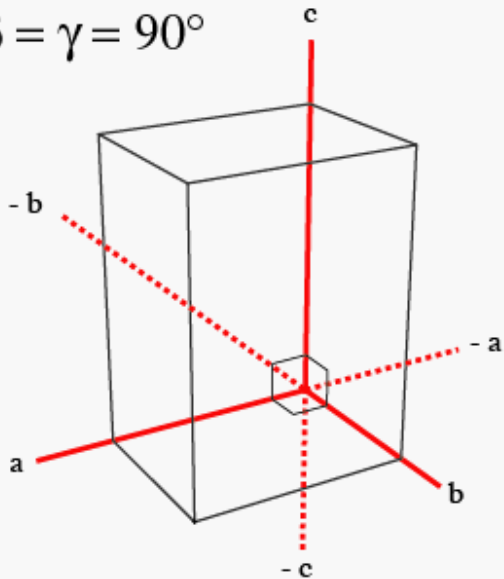
$$e_K = \sum_i K_i m_i^2 + \sum_{ij} K_{ij} m_i^2 m_j^2 + K_{123} m_1^2 m_2^2 m_3^2 + \sum_{ij} K'_{ij} m_i^4 m_j^4 + \dots$$

Ejemplo: sistema ortorrómbico

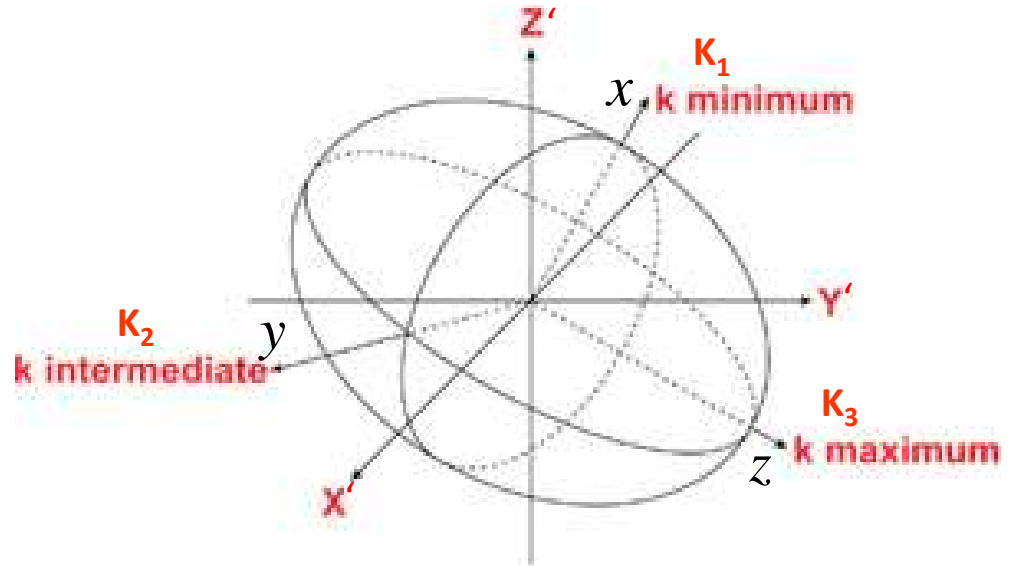
Orthorhombic

$a \neq b \neq c$

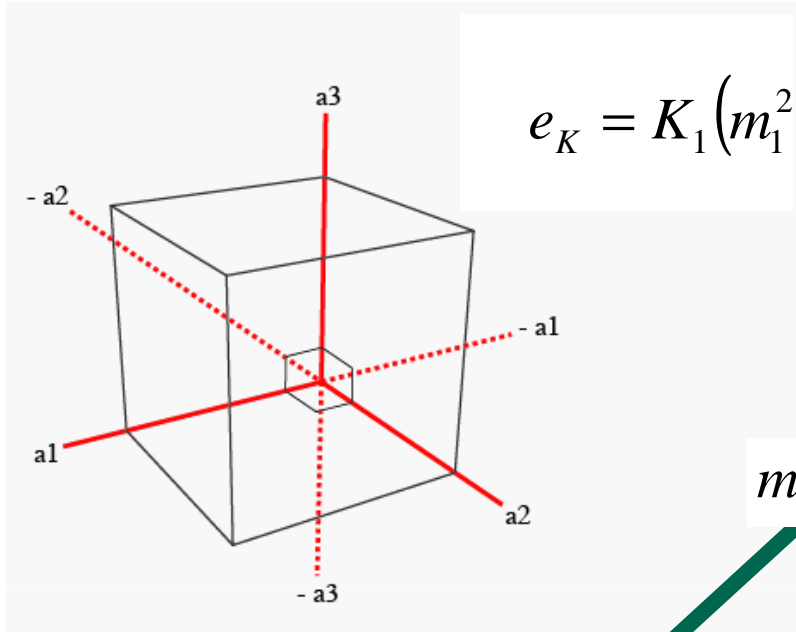
$\alpha = \beta = \gamma = 90^\circ$



$$e_K \approx K_1 m_1^2 + K_2 m_2^2 + K_3 m_3^2$$



sistema cúbico



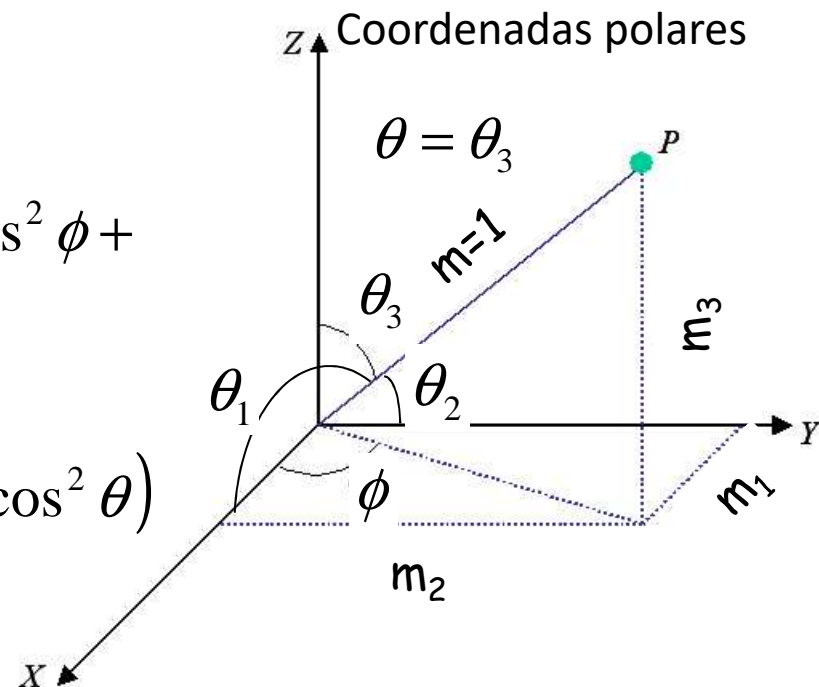
$$e_K = K_1 (m_1^2 m_2^2 + m_1^2 m_3^2 + m_2^2 m_3^2) + K_2 m_1^2 m_2^2 m_3^2$$

$$m_i = \cos \theta_i$$

$$e_K = (K_1 + K_2 \cos^2 \theta) \sin^4 \theta \sin^2 \phi \cos^2 \phi + K_1 \sin^2 \theta \cos^2 \theta$$

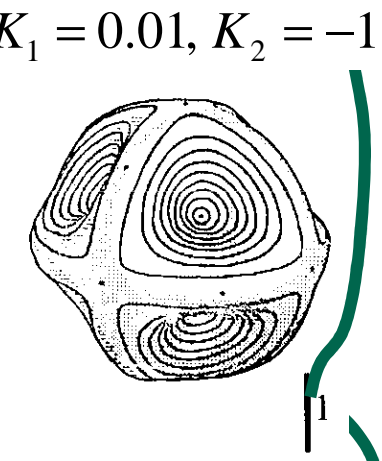
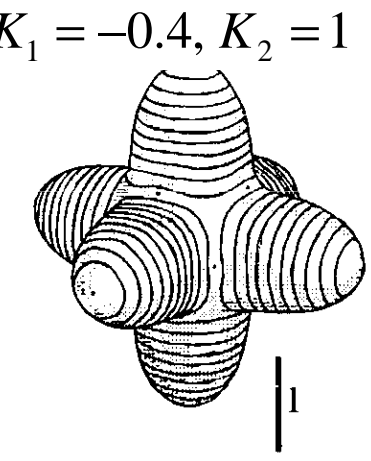
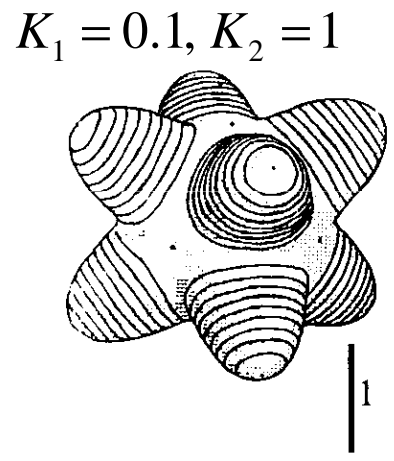
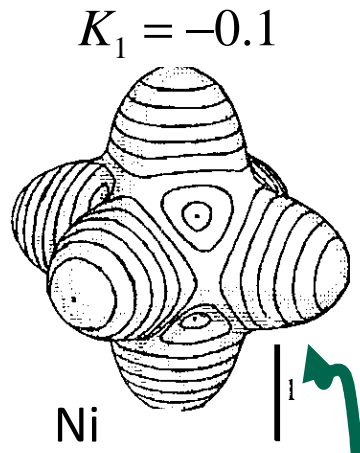
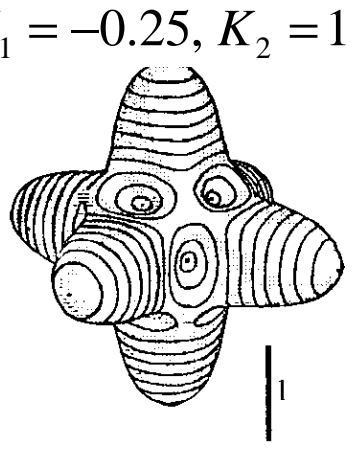
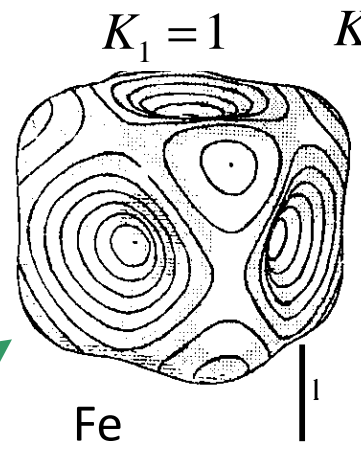
$$e_{K_1} = K_1 \sin^2 \theta (\sin^2 \theta \sin^2 \phi \cos^2 \phi + \cos^2 \theta)$$

$$e_{K_2} = K_2 \cos^2 \theta \sin^4 \theta \sin^2 \phi \cos^2 \phi$$



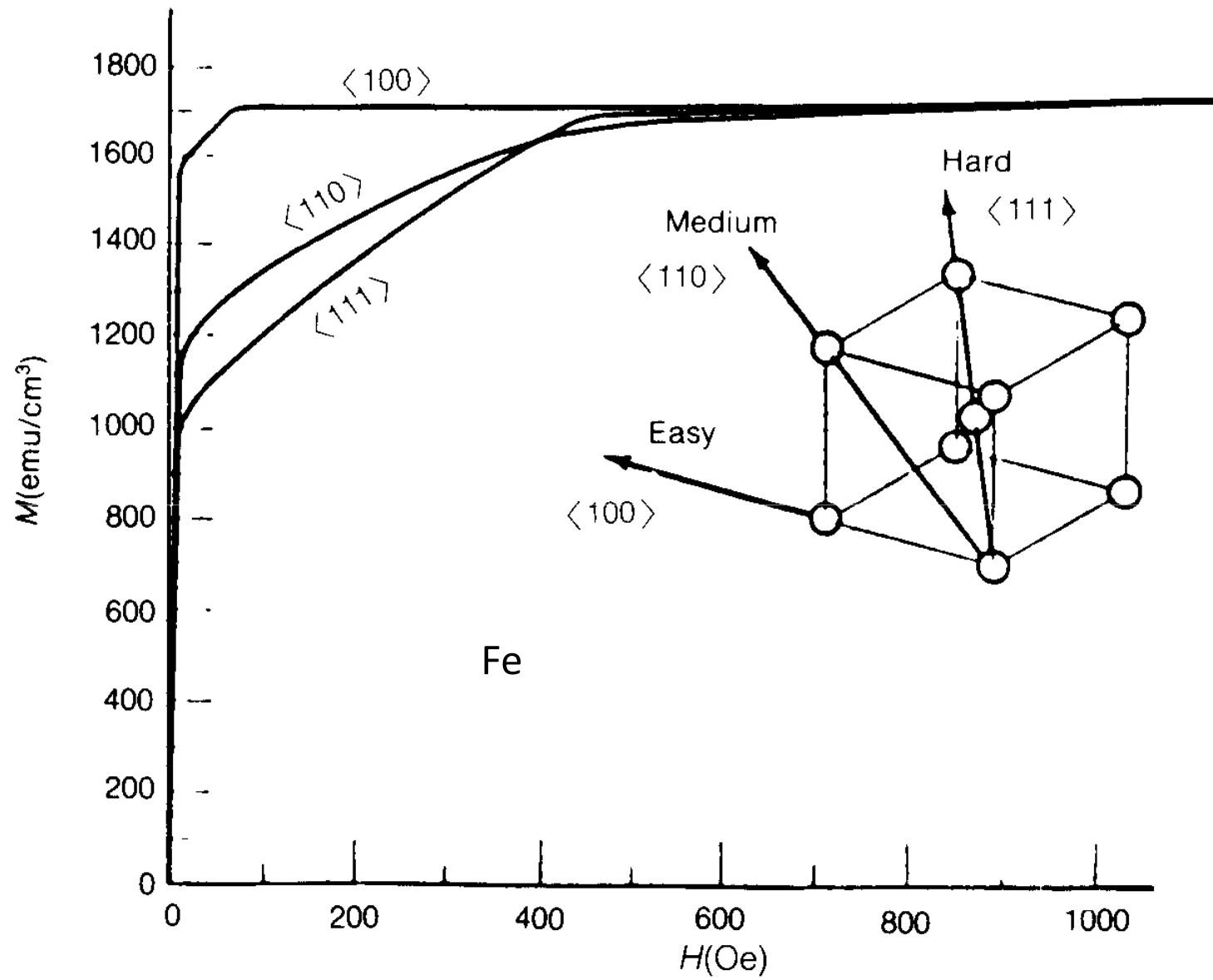
sistema cúbico
Curvas de energía
constante

$$e_K = K_1(m_1^2 m_2^2 + m_1^2 m_3^2 + m_2^2 m_3^2) + K_2 m_1^2 m_2^2 m_3^2$$

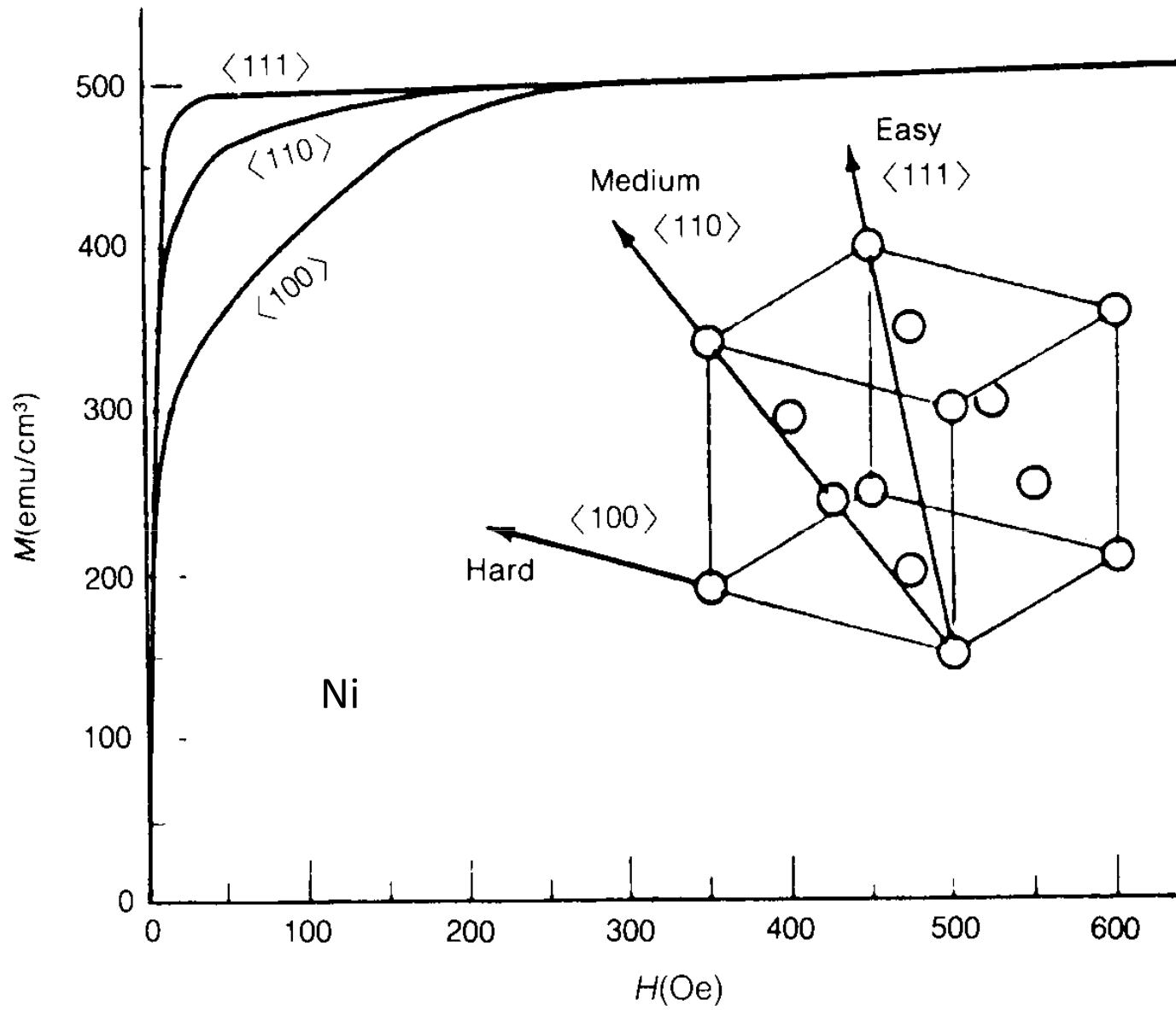


Material	K_1 (10^5 J/m ³)	K_2 (10^5 J/m ³)	Eje fácil
Fe	0.480	0.05	(100)
Ni	-0.045	-0.023	(111)

sistema cúbico

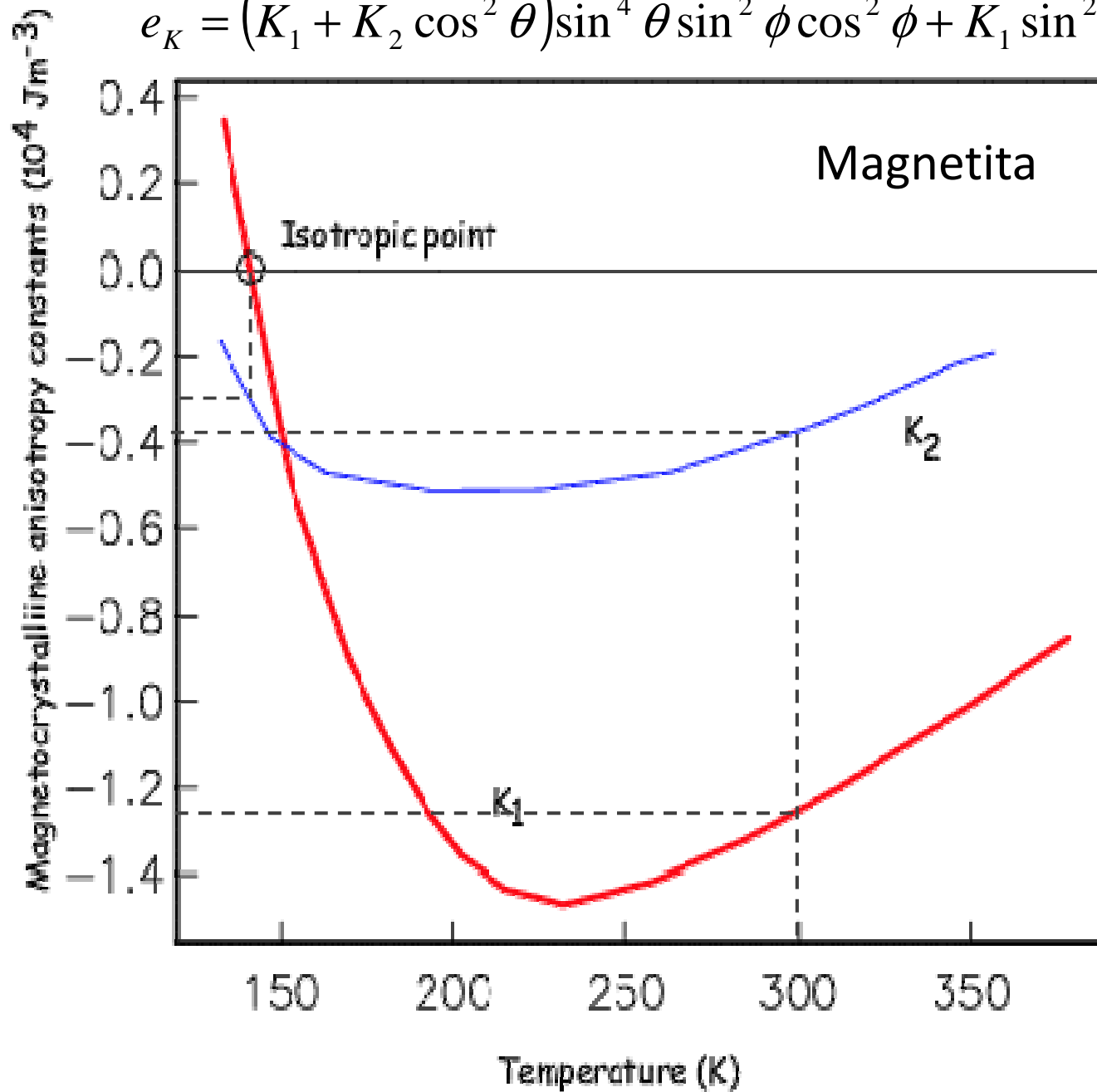


sistema cúbico

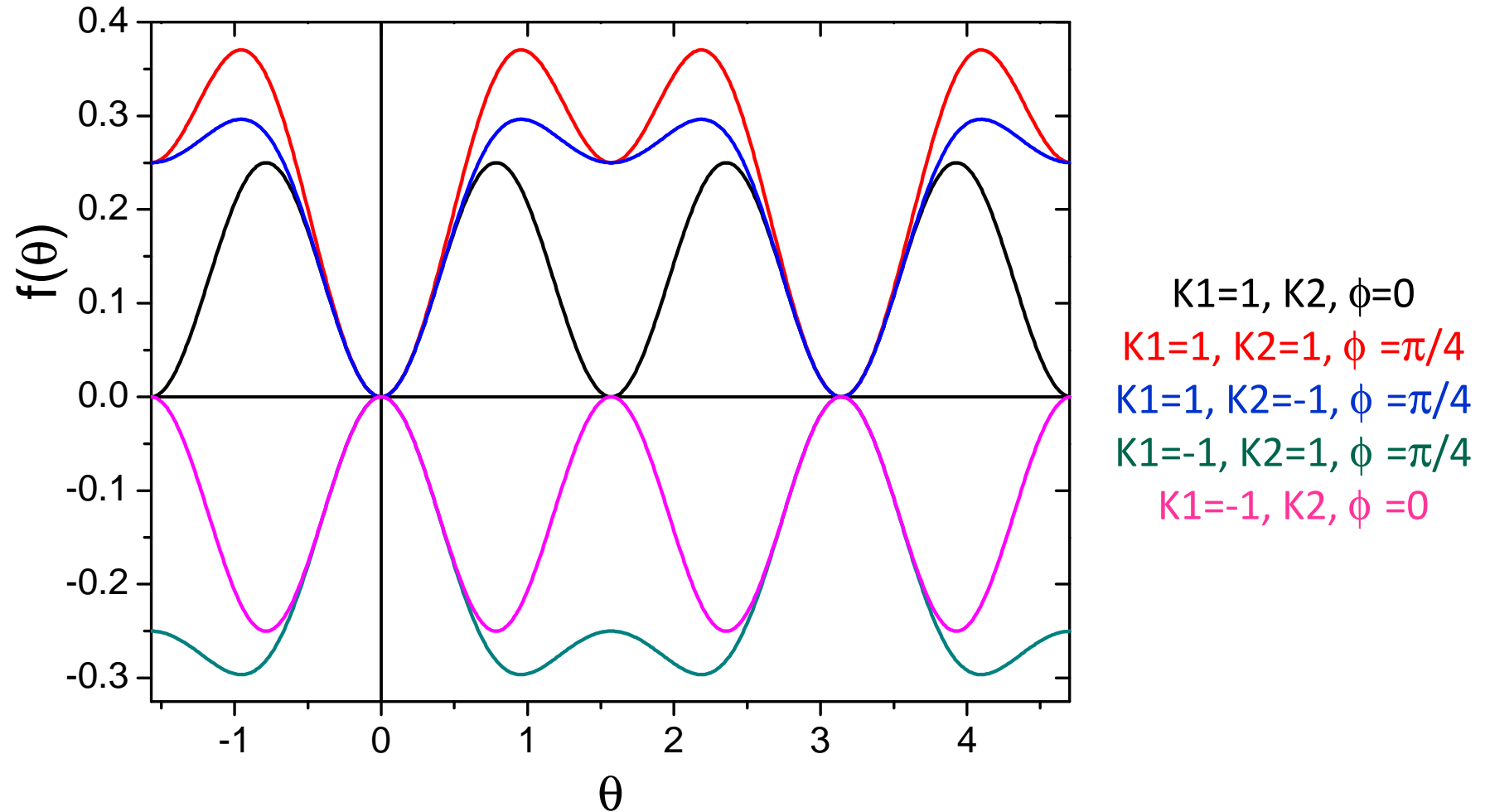


sistema cúbico

$$e_K = (K_1 + K_2 \cos^2 \theta) \sin^4 \theta \sin^2 \phi \cos^2 \phi + K_1 \sin^2 \theta \cos^2 \theta$$

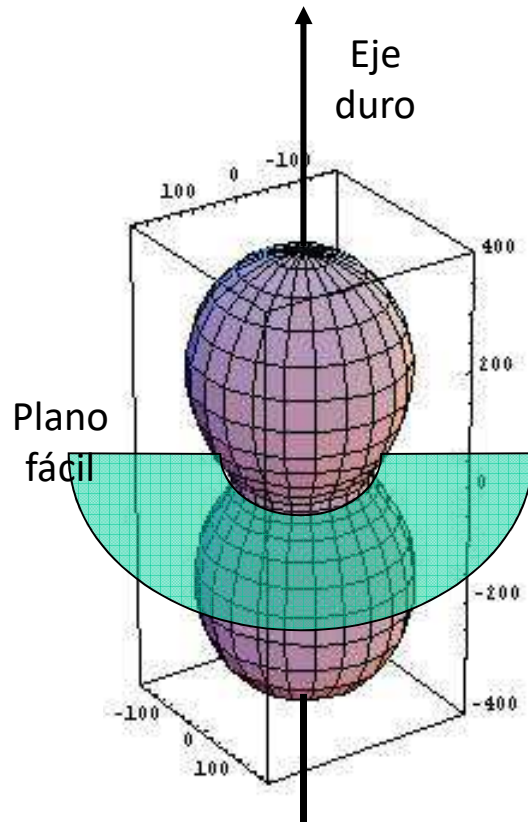
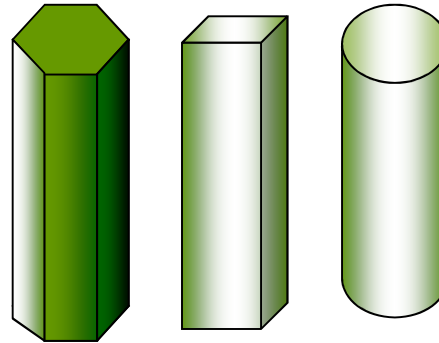


sistema cúbico

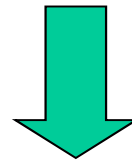


$$e_K = (K_1 + K_2 \cos^2 \theta) \sin^4 \theta \sin^2 \phi \cos^2 \phi + K_1 \sin^2 \theta \cos^2 \theta$$

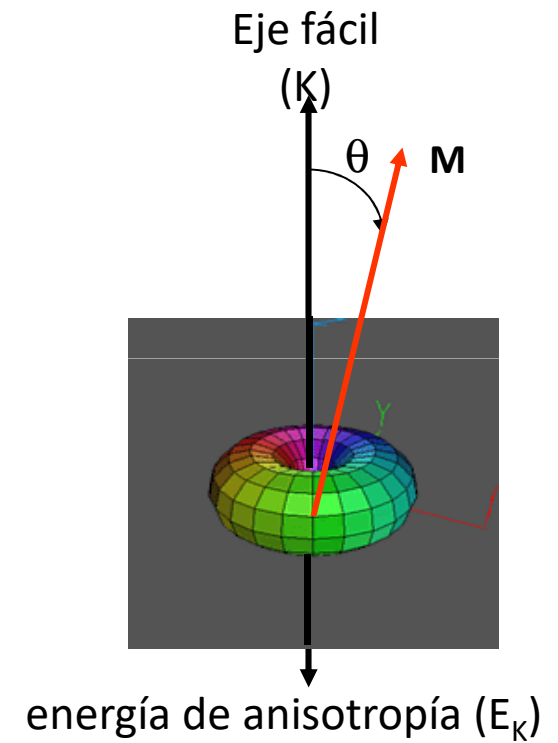
Sistemas hexagonal y tetragonal



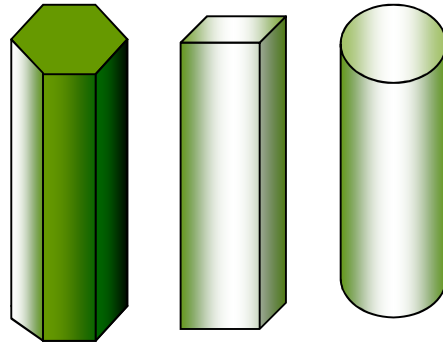
$$e_K = K_1 \cos^2 \theta + K_2 \cos^4 \theta$$



$$e_K = K_1' \sin^2 \theta + K_2' \sin^4 \theta$$

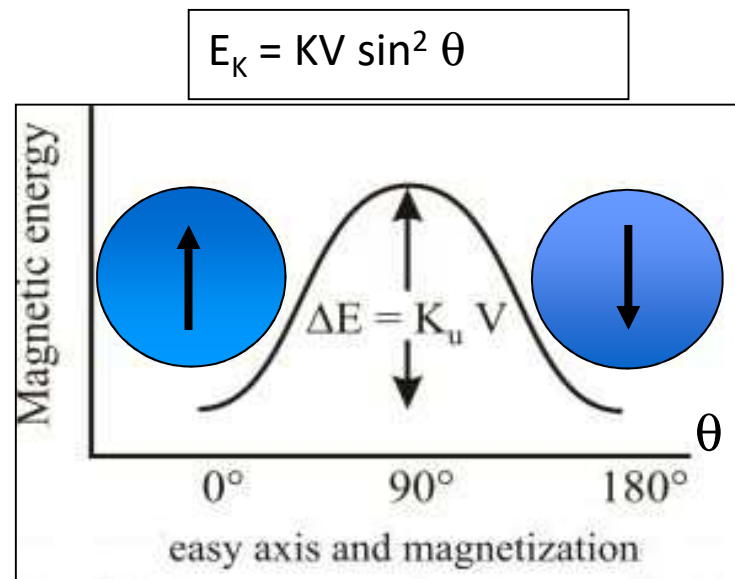


Anisotropía uniaxial



$$e_K = K_1 \sin^2 \theta + K_2 \sin^4 \theta \longrightarrow e_K = K \sin^2 \theta$$

Siempre que pueda simplificarse



Anisotropía uniaxial

ejemplos

$$e_K = K_1 \sin^2 \theta + K_2 \sin^4 \theta$$

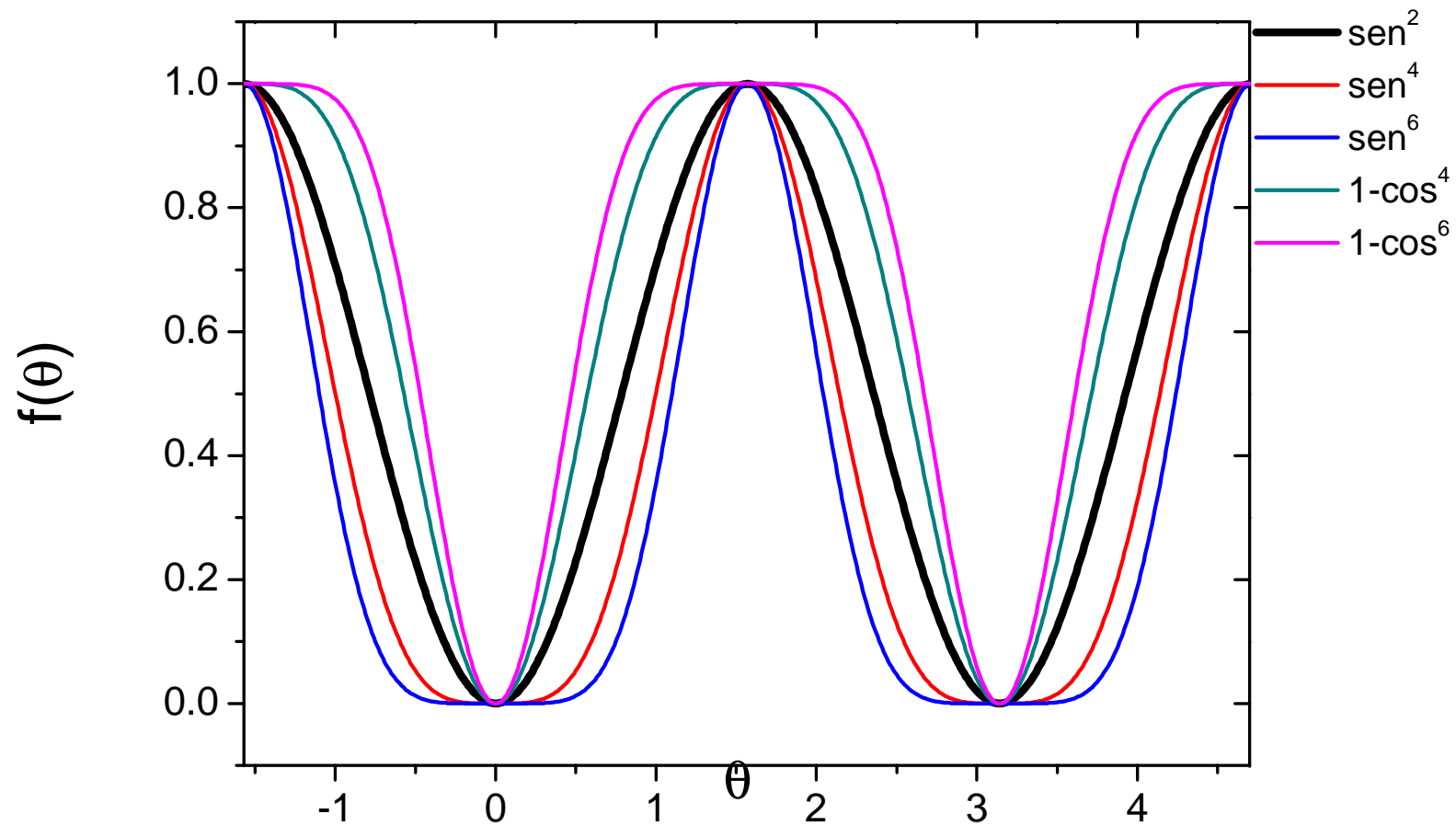
Material	K_1 (10^5 J/m ³)	K_2 (10^5 J/m ³)	Eje fácil
Co	4.1	1.0	hexagonal
SmCo ₅	1100	-	hexagonal

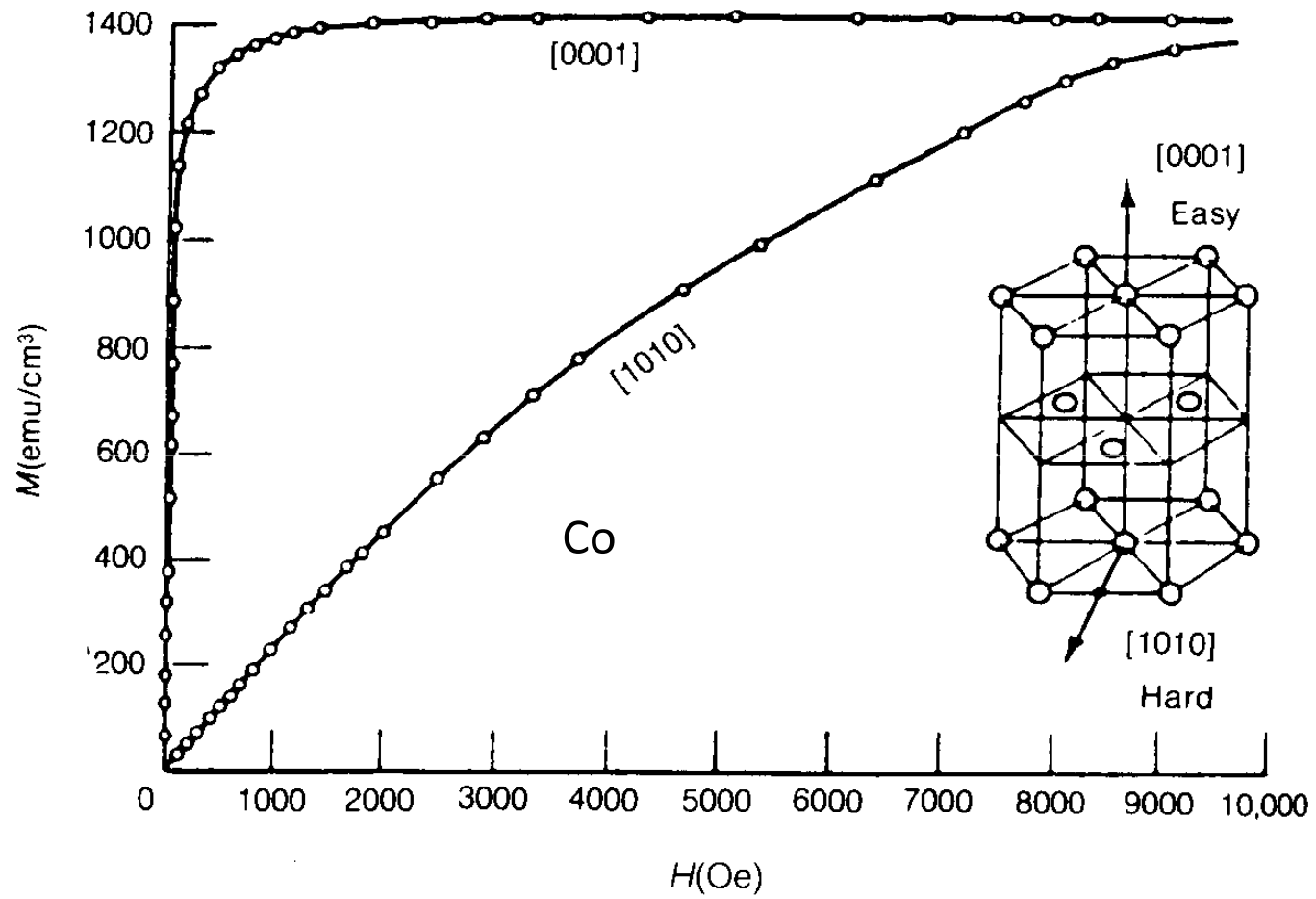
Anisotropía uniaxial

Efecto de las potencias de seno y coseno

$$e_K = K \sin^n \theta$$

$$e_K = K(1 - \cos^n \theta)$$

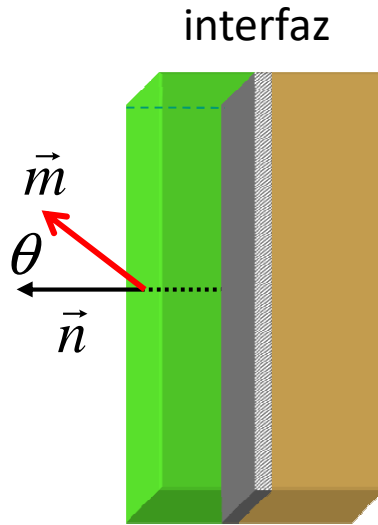




Anisotropía de Interfaz
Anisotropía de Intercambio

superficies e interfaces

Anisotropía de interfaz



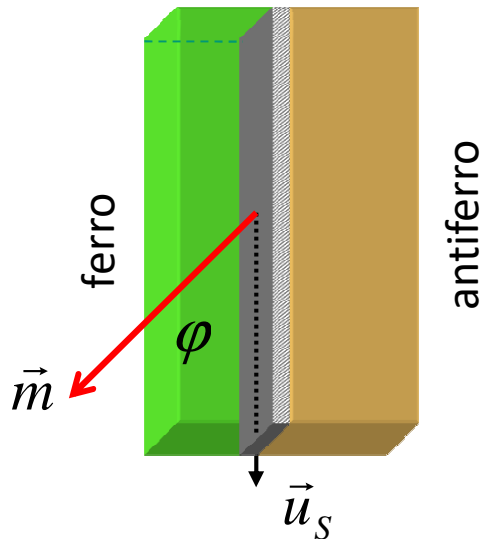
$$\vec{m} = \vec{M} / M$$

$$e_K = K_S [1 - (\vec{m} \cdot \vec{n})^2]$$

$$(e_K = K_S [1 - (\cos \theta)^2])$$

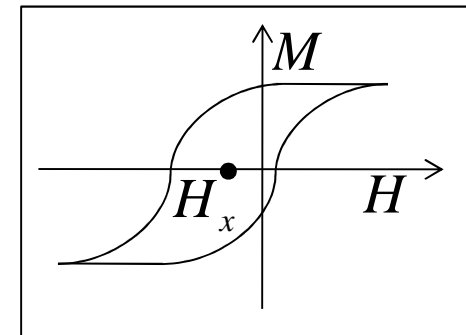
$$\left. \begin{array}{l} K_S > 0 \Rightarrow \vec{m} // \text{sup} \\ K_S < 0 \Rightarrow \vec{m} \perp \text{sup} \end{array} \right\}$$

Anisotropía de intercambio*



$$e_K = K_S \vec{m} \cdot \vec{u}_S = \frac{H_x}{2} \vec{m} \cdot \vec{u}_S$$

$$e_K = \frac{H_x}{2} m \cos \varphi$$



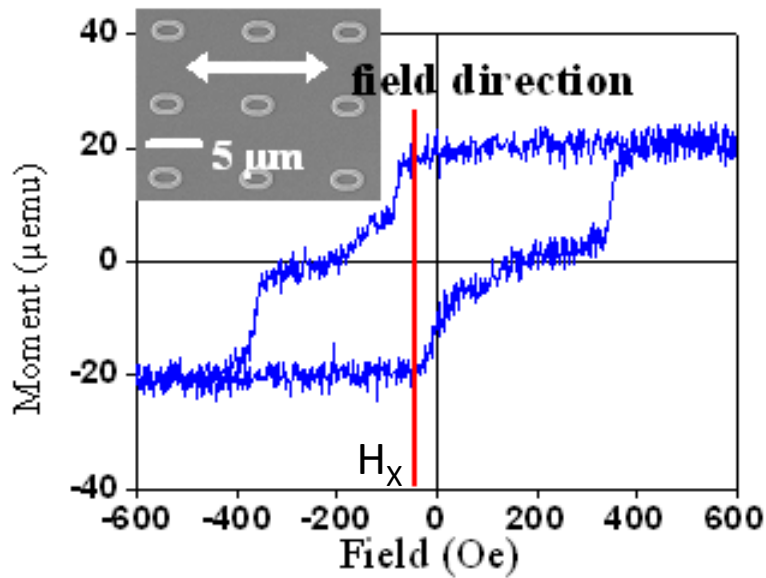
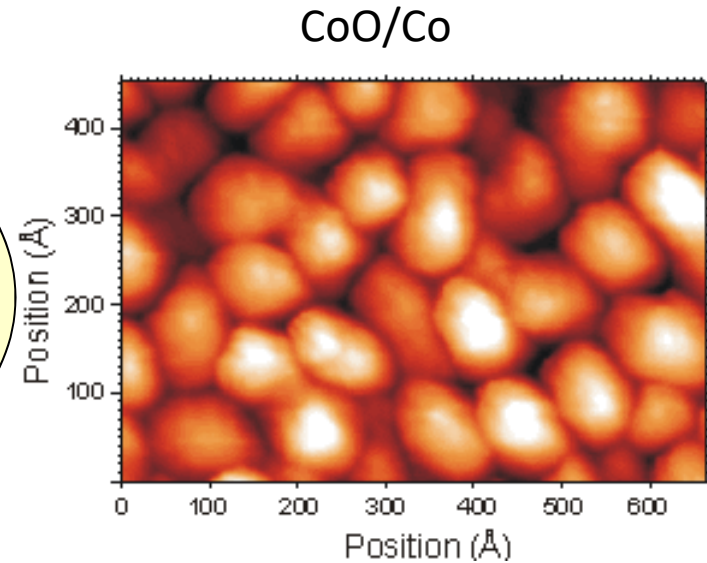
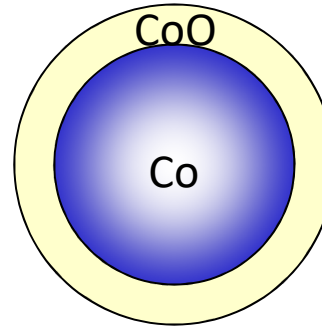
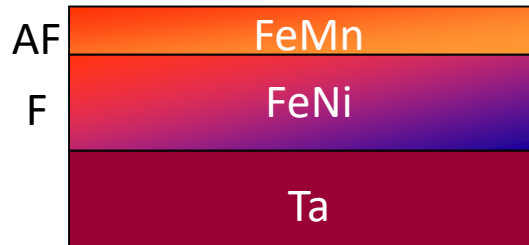
Exchange bias field

*también llamada unidireccional

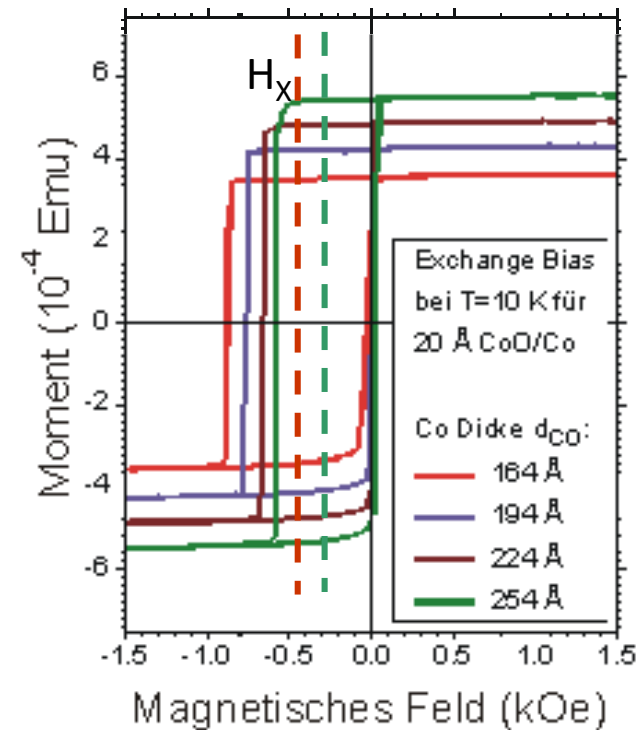
Anisotropía de intercambio

Observación del exchange bias

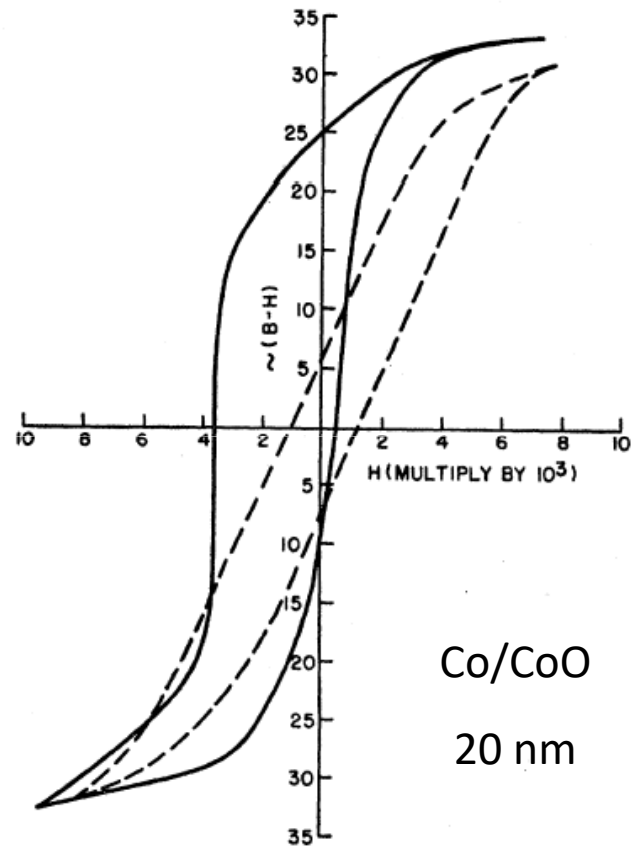
$$e_K = K_S \vec{m} \cdot \vec{u}_S = \frac{H_x}{2} \vec{m} \cdot \vec{u}_S$$



Ta 20nm / NiFe 20nm / FeMn 10 nm film



In the
news... 



Letters to the Editor

New Magnetic Anisotropy

W. H. MEIKLEJOHN AND C. P. BEAN

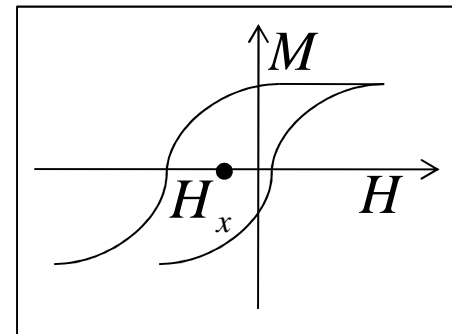
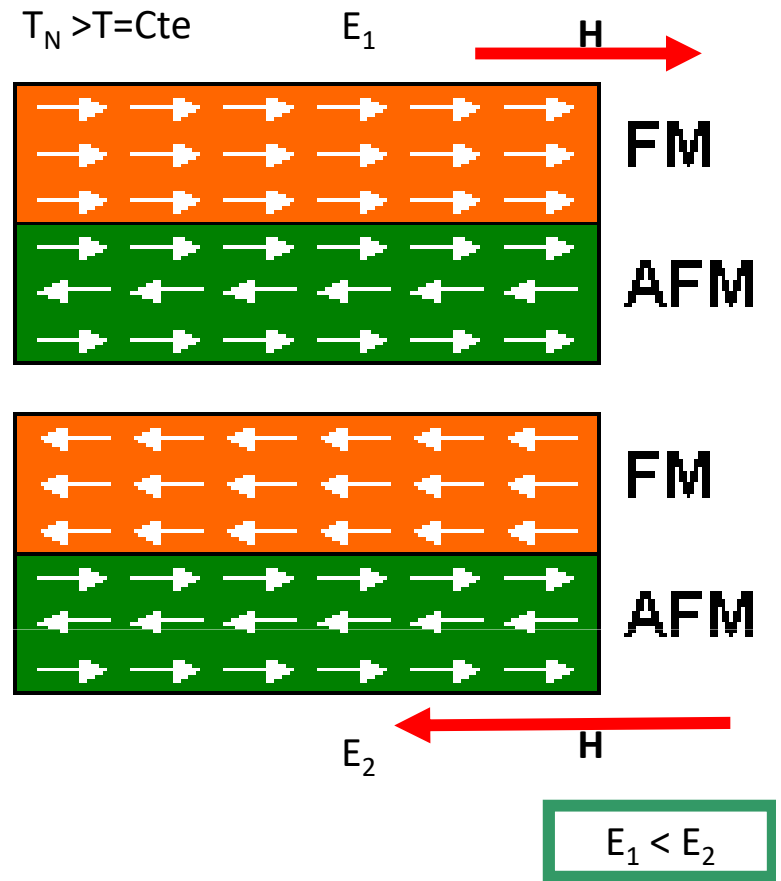
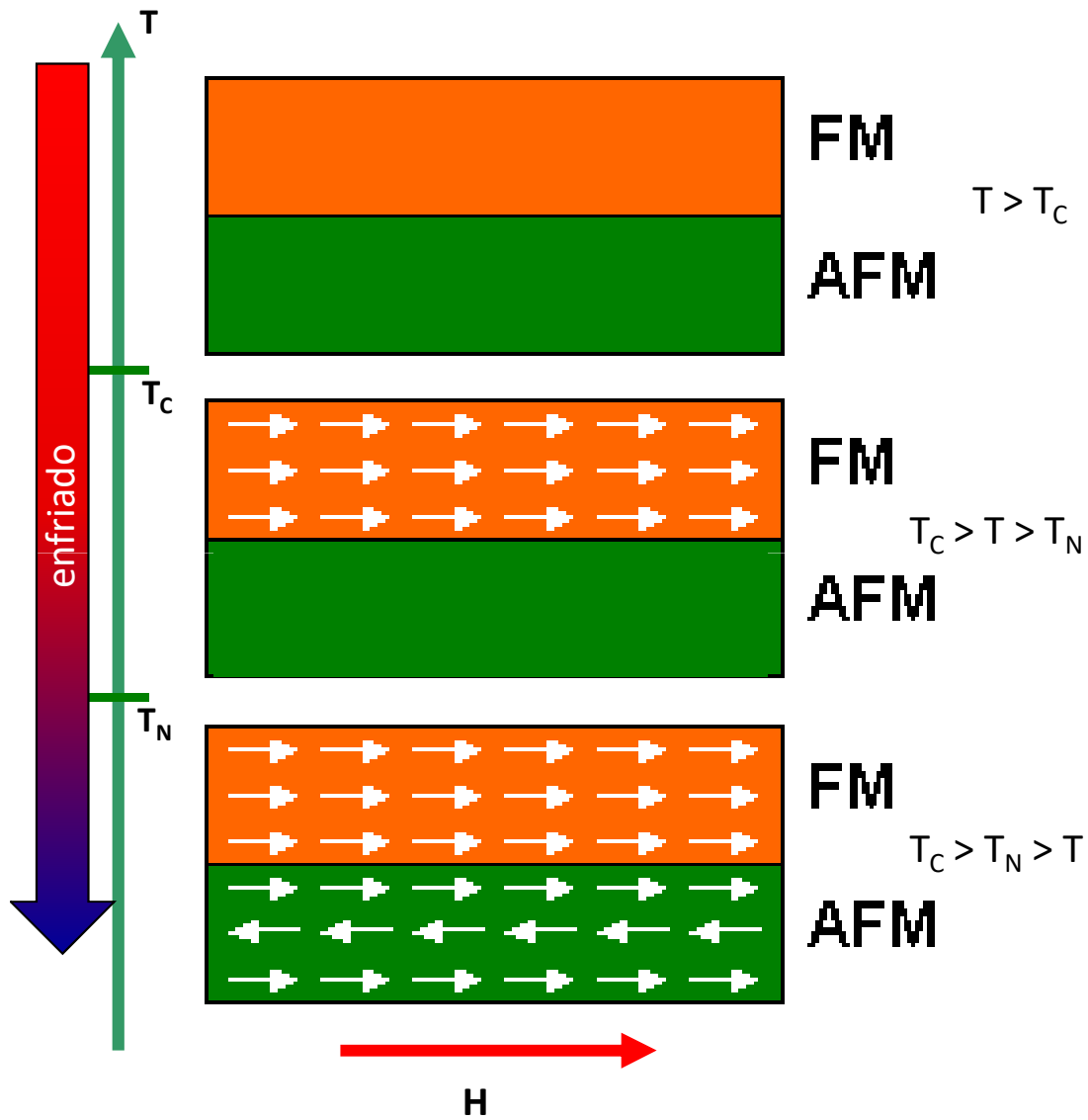
General Electric Research Laboratory, Schenectady, New York

(Received March 7, 1956)

PHYSICAL REVIEW

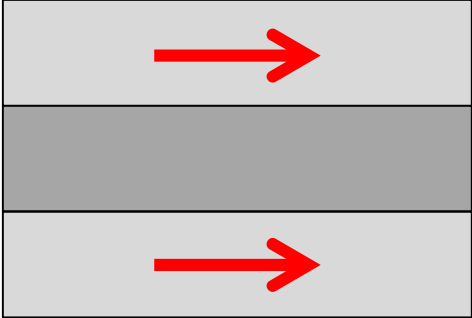
VOLUME 102, NUMBER 5

JUNE 1, 1956

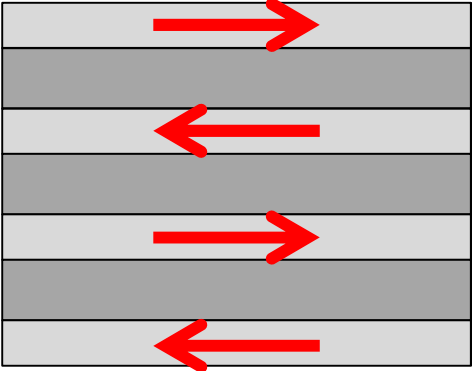
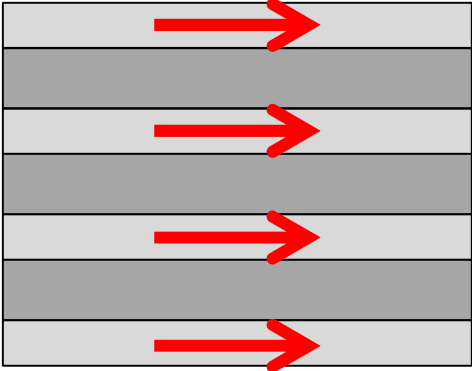
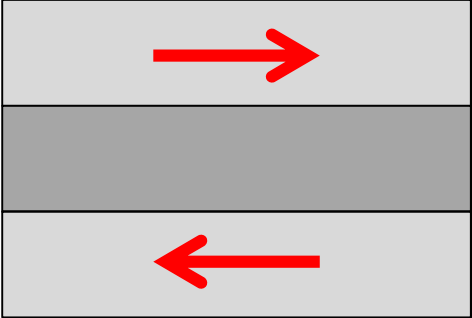


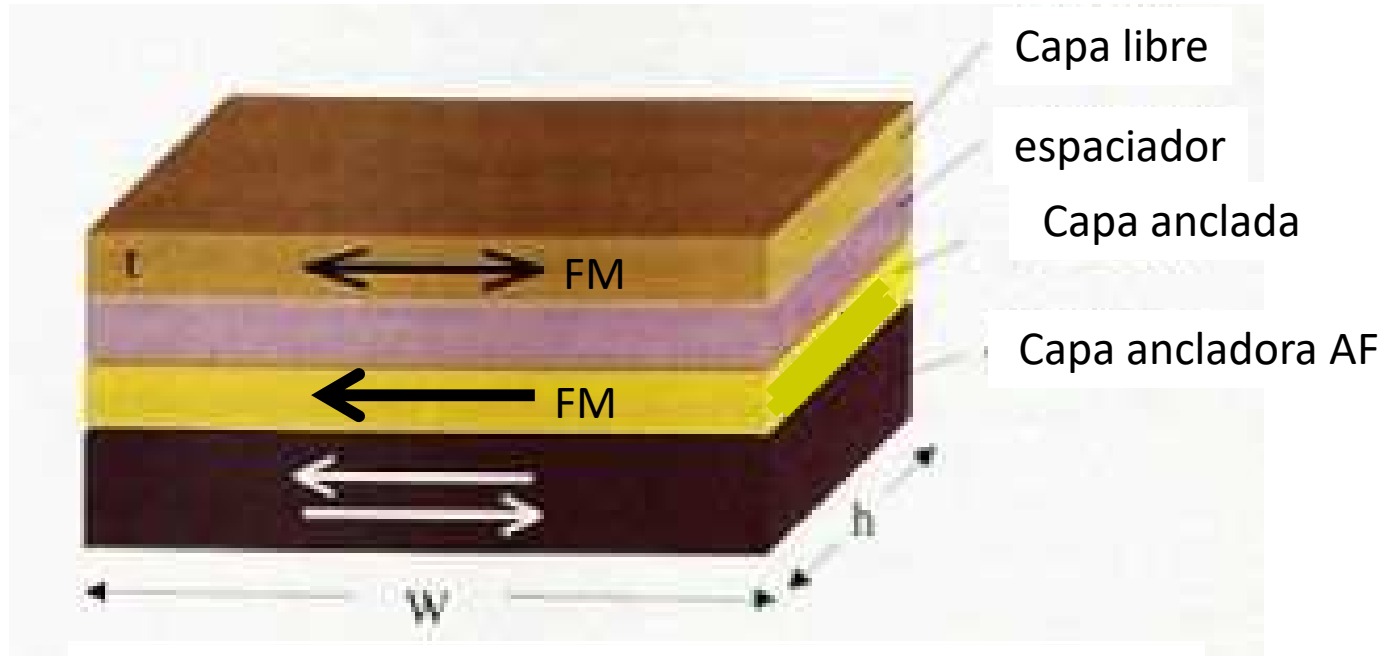
Magnetoresistencia

baja resistencia

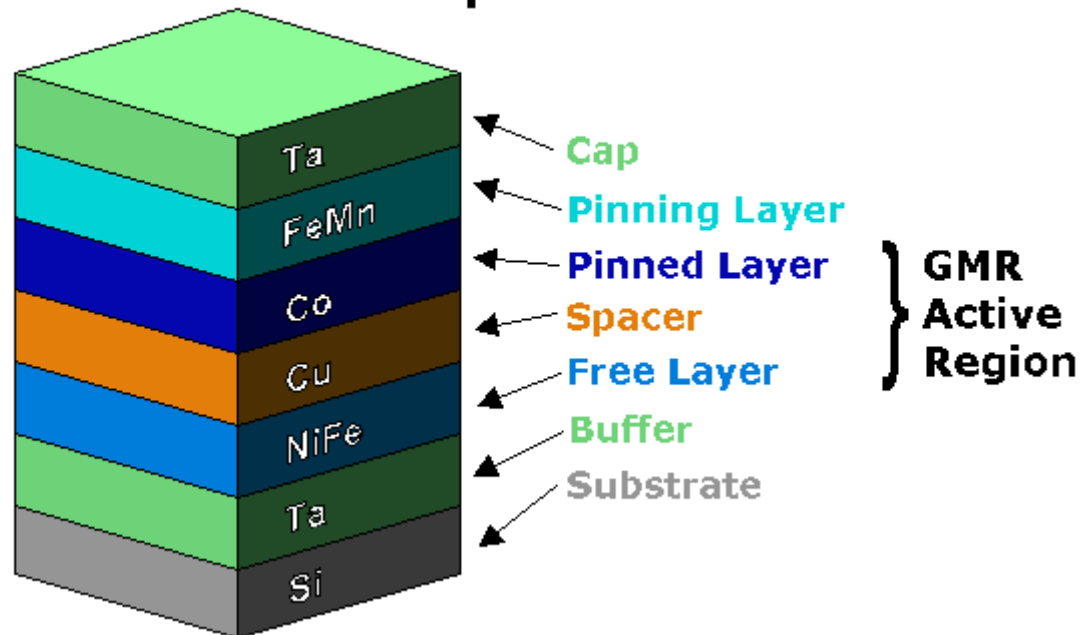


alta resistencia

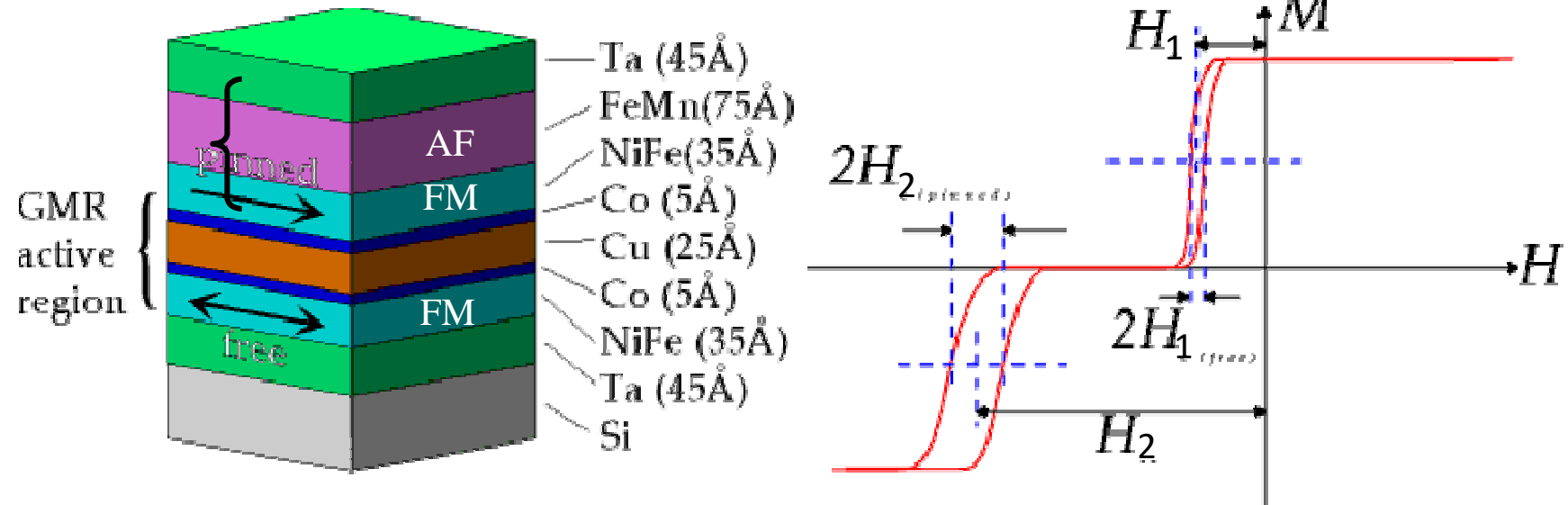




Spin Valve Structure

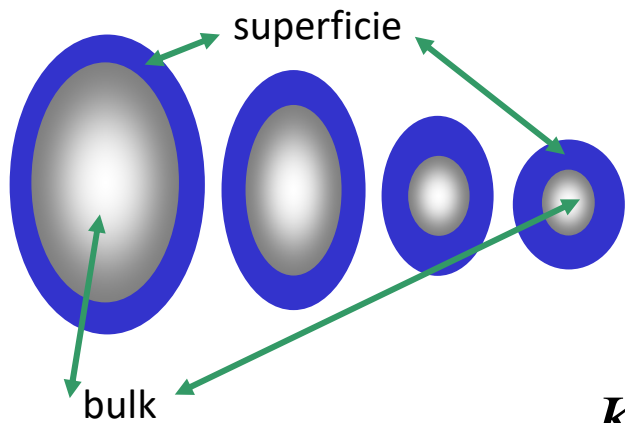


Válvula de spin



Anisotropía en nanopartículas magnéticas

anisotropía de superficie en nanopartículas



$K_s = 10^{-4}-10^{-3} \text{ J/m}^2$,
energía de anisotropía
por unidad de área
superficial

$$K_{ef} = K_B + K_{V_s}^{ef}$$

$$K_{V_s}^{ef} \approx \frac{SK_s}{V} \approx \frac{4\pi r^2}{\frac{4}{3}\pi r^3} K_s = \frac{3}{r} K_s = \frac{6}{d} K_s$$

Partícula esférica

superficies/interfaces:

- discontinuidad composicional y configuracional
- mayor efecto anisotrópico

$$K_{ef} = K_B + \frac{6K_s}{d}$$

$$K_{ef} = K_B + \gamma \frac{K_s}{d}$$

Bødker et. Al (1994)

Anisotropía de superficie - ejemplo

$$K_B(\text{Co}_{fcc}) \approx 1 \times 10^5 \text{ J} / \text{m}^3$$

$$K_S(\text{Co} / \overset{\text{Alúmina}}{\text{Al}_2\text{O}_3}) \approx 3.3 \times 10^{-4} \text{ J} / \text{m}^2$$

$$K_{ef} = K_B + \gamma \frac{K_s}{d}$$

$$K_{ef}(\text{Co} / \text{Al}_2\text{O}_3) \approx \left[1 \times 10^5 + 6 \frac{3.3 \times 10^{-4}}{11 \times 10^{-9}} \right] \text{ J} / \text{m}^3 \approx 2.8 \times 10^5 \text{ J} / \text{m}^3$$

Si $d \sim 3 \text{ nm} = 3 \times 10^{-9} \text{ m}$

$$\Rightarrow K_{ef}(\text{Co} / \text{Al}_2\text{O}_3) \approx 10^6 \text{ J} / \text{m}^3$$

$$\tau = \tau_0 e^{\frac{K_{ef} V}{kT}}$$

Mayores tiempos de relajación

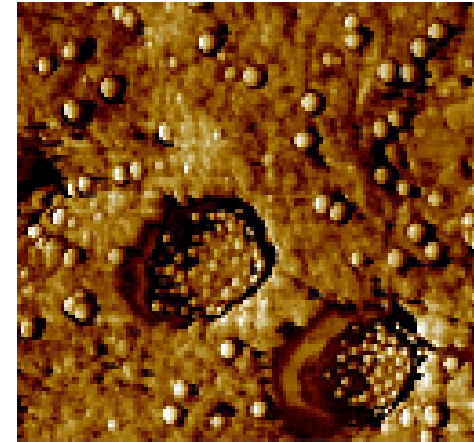
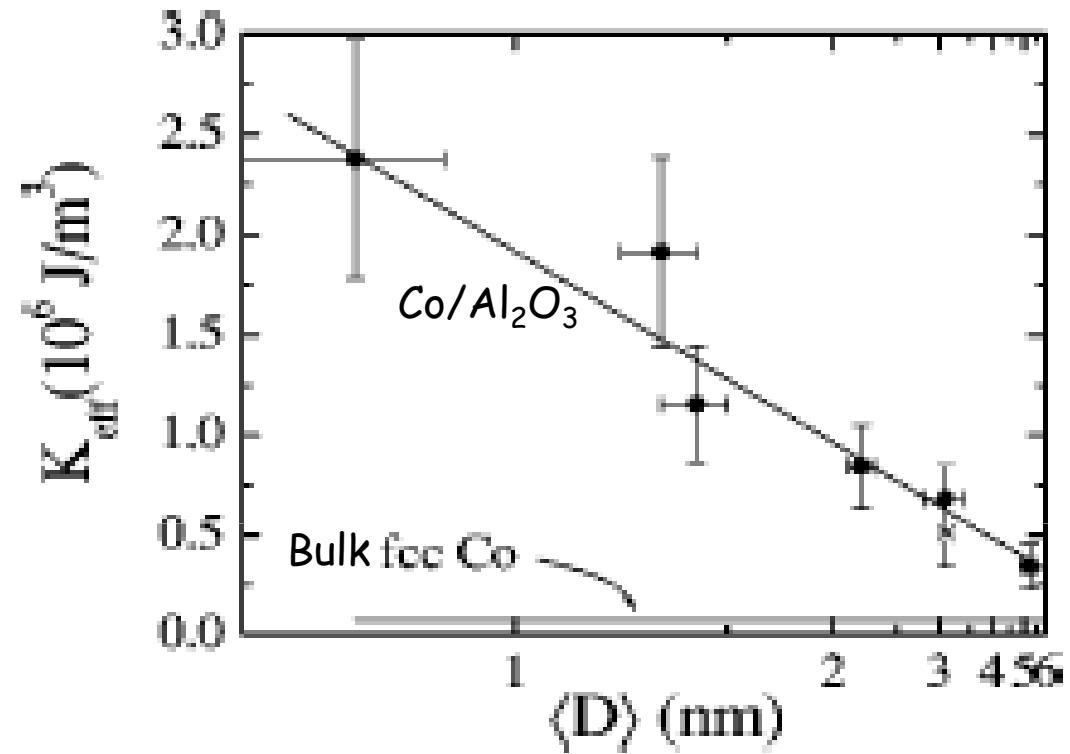


imagen MFA de nanopartículas de Co fcc en una matriz de alúmina. Las partículas son de aprox 11 nm (diámetro).



F. Luis, J.M. Torres, L.M. Gracia, J. Bartolomé, J. Stankiewicz, F. Petroff, F. Fettar, J. L. Maurice and A. Vaurés. Phys. Rev B, **65** (2002) 094409

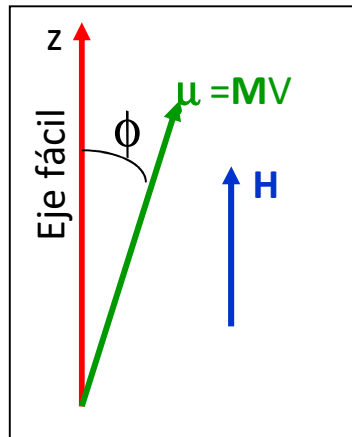
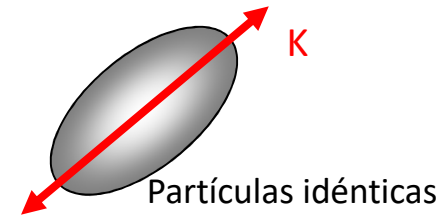
Modelo de Stoner - Wohlfarth

$$T = 0K$$

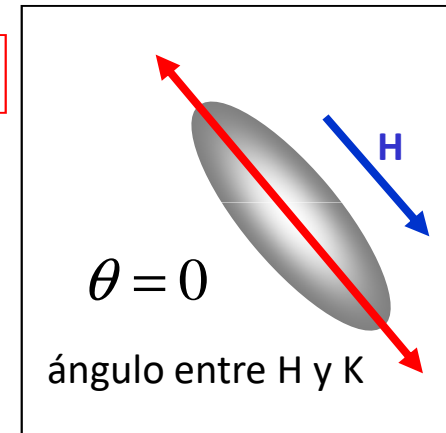
monodominio

Anisotropía uniaxial

no interactuantes



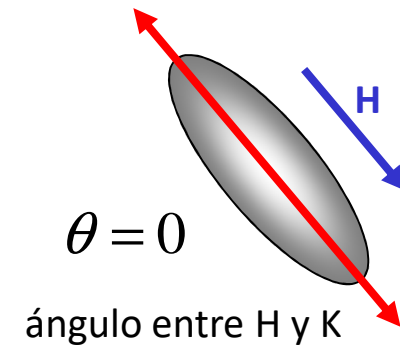
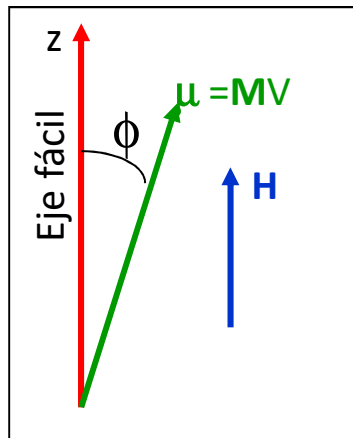
Campo paralelo al eje fácil



$$E_K = e_K V = KV \sin^2 \phi$$

$$E_H = -\vec{\mu} \cdot \vec{B} = -\mu_0 \vec{\mu} \cdot \vec{H} = -\mu_0 V M_z H = -\mu_0 V M_S H \cos \phi$$

$$E = E_K + E_H = KV \sin^2 \phi - \mu_0 V M_S H \cos \phi$$



$$E = E_K + E_H = KV \sin^2 \phi - \mu_0 VM_S H \cos \phi$$

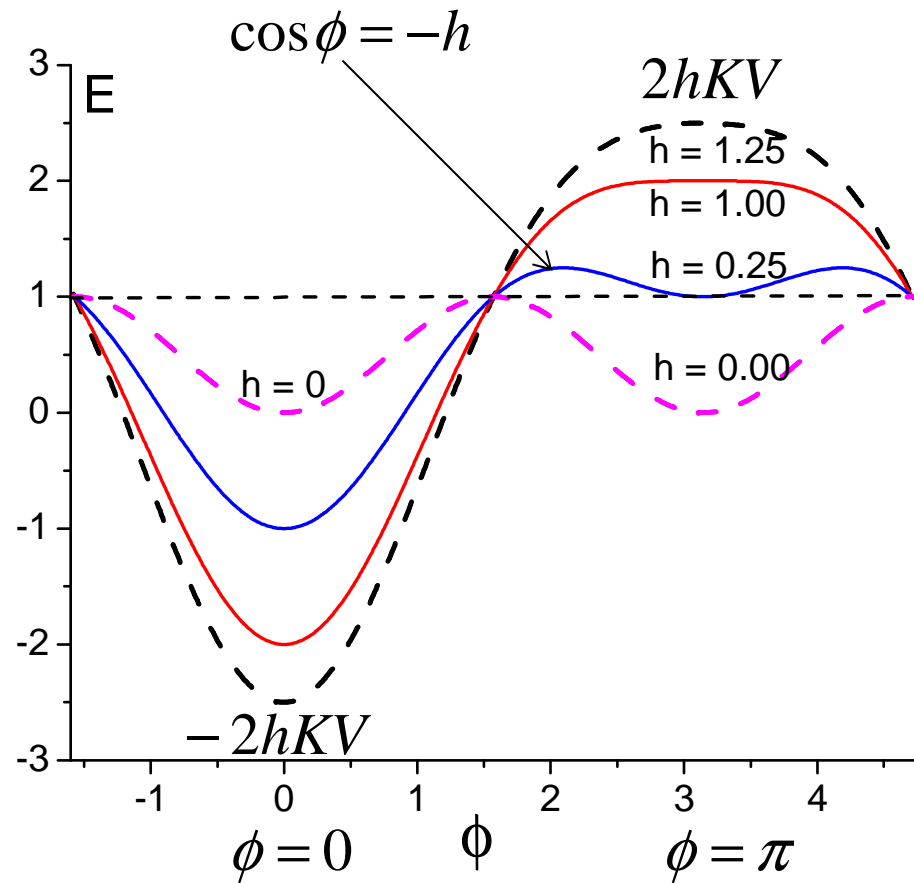
llamamos Campo de anisotropía

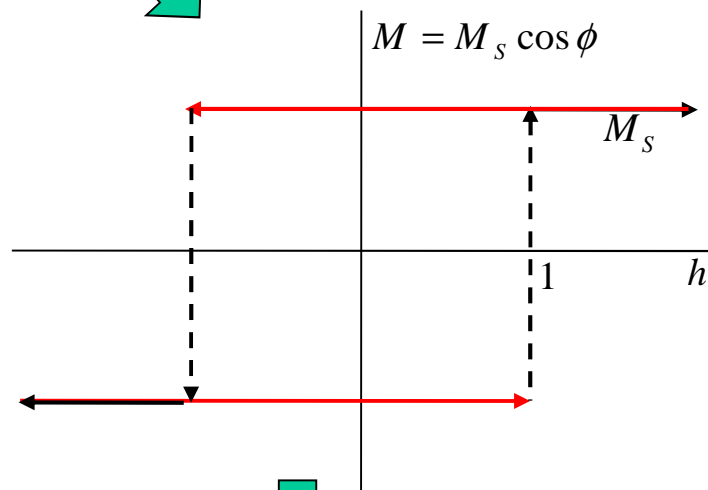
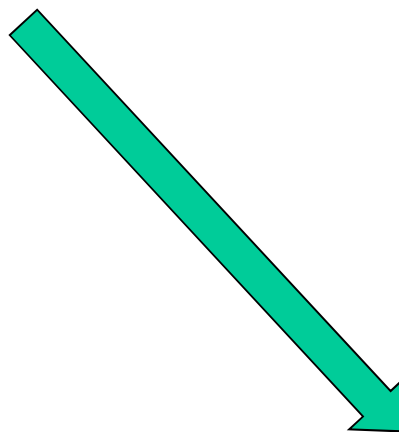
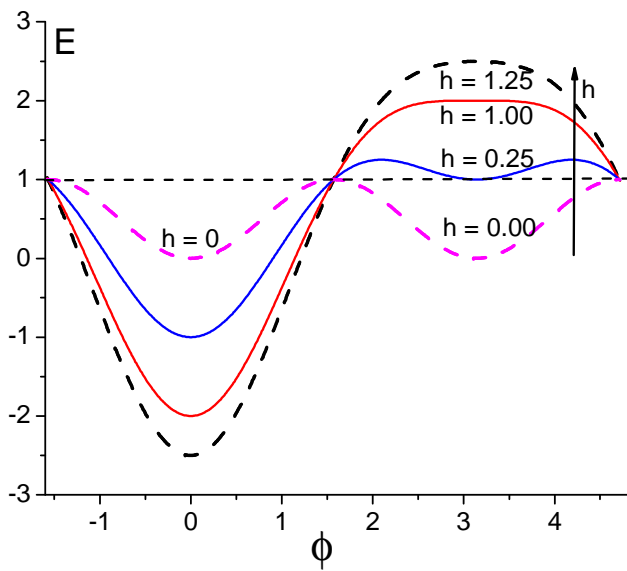
$$H_K = \frac{2K}{\mu_0 M_S} \quad h = \frac{H}{H_K} = \frac{\mu_0 M_S H}{2K}$$

$$E = KV (\sin^2 \phi - 2h \cos \phi)$$

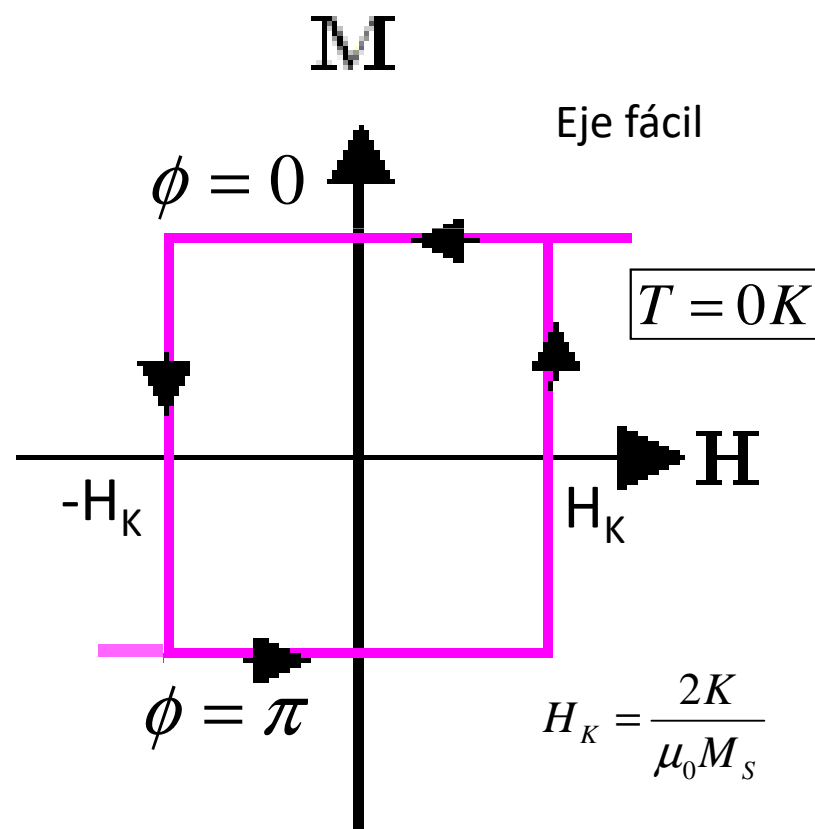
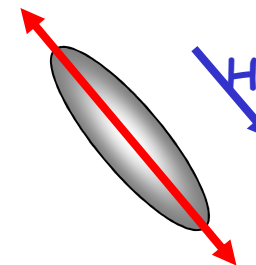
$$E = KV(\sin^2 \phi - 2h \cos \phi)$$

$$h = \frac{H}{H_K} \quad H_K = \frac{2K}{\mu_0 M_S}$$



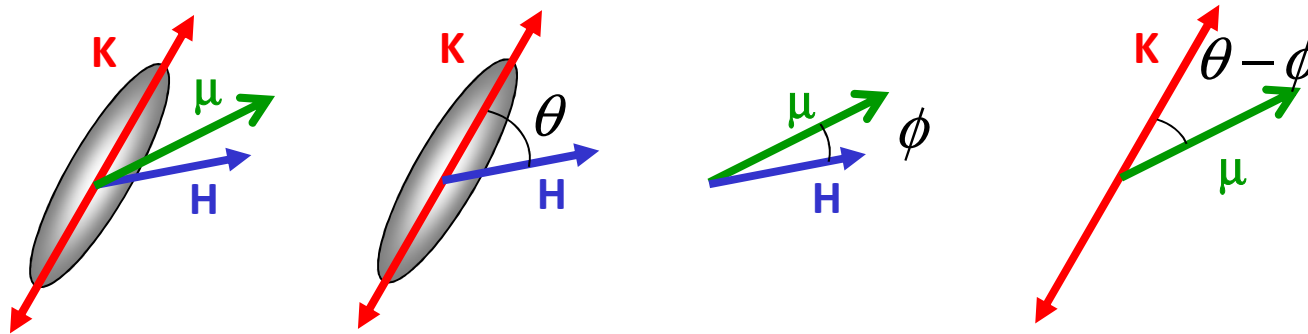


$$M_z = M_s \cos \theta$$

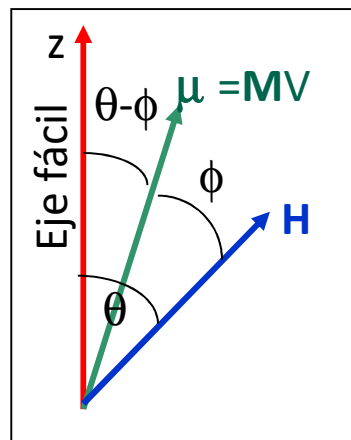


Campo en dirección arbitraria

$$\theta \neq 0$$

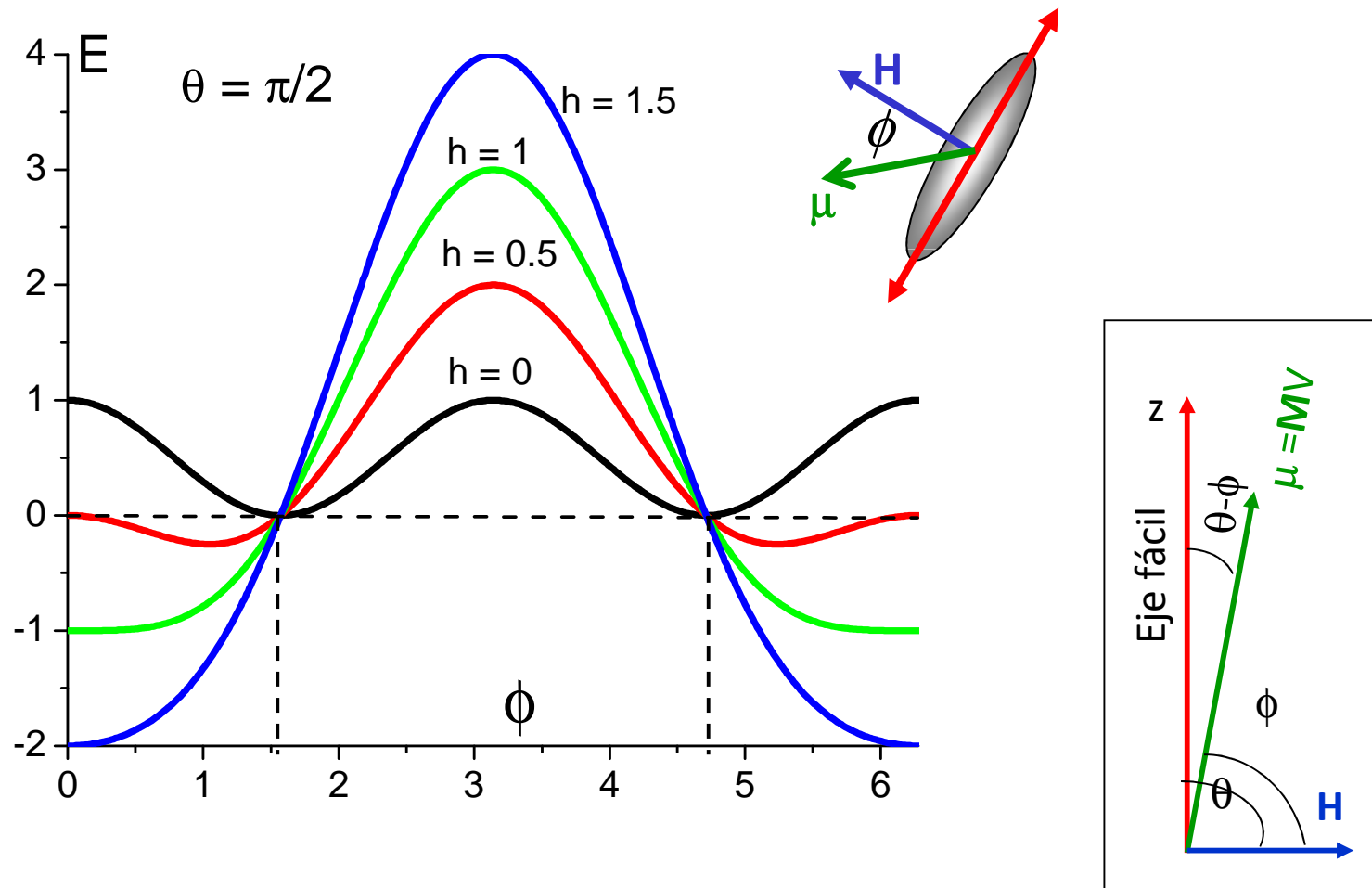


$$E = E_K + E_H = KV[\sin^2(\phi - \theta) - 2h\cos\phi]$$

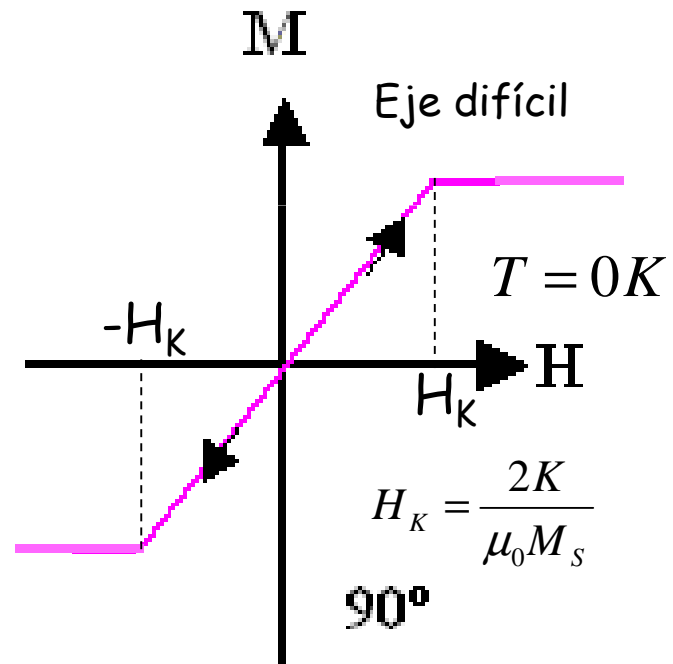
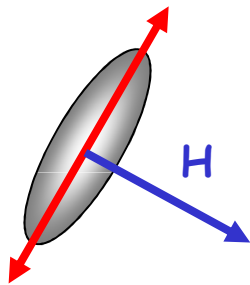


$$\theta = \pi / 2$$

$$E = E_K + E_H = KV \cos \phi (\cos(\phi) - 2h)$$

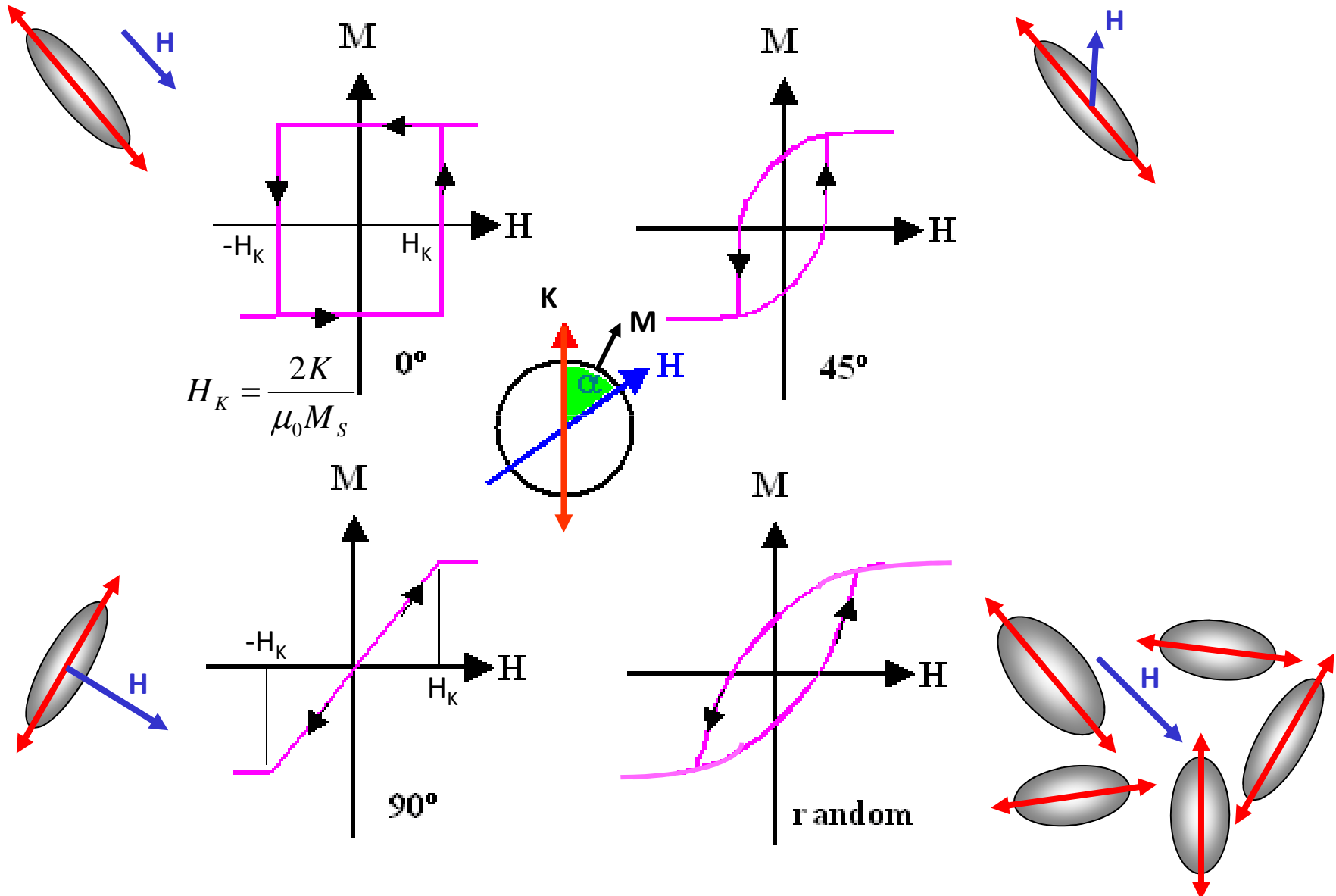


$$M_z = \frac{M_S}{H_K} H; \quad |h| < 1$$



Partículas ferromagnéticas pequeñas – modelo de Stoner - Wohlfarth

régimen bloqueado → T = 0 K



E.C. Stoner y E.P. Wohlfarth, IEEE Transactions on Magnetics **27**, 3475-3518 (1991)

[599]

A MECHANISM OF MAGNETIC HYSTERESIS IN
HETEROGENEOUS ALLOYS

By E. C. STONER, F.R.S. AND E. P. WOHLFARTH
Physics Department, University of Leeds

(Received 24 July 1947)

VOL. 240. A. 826 (Price 10s.)

74

[Published 4 May 1948



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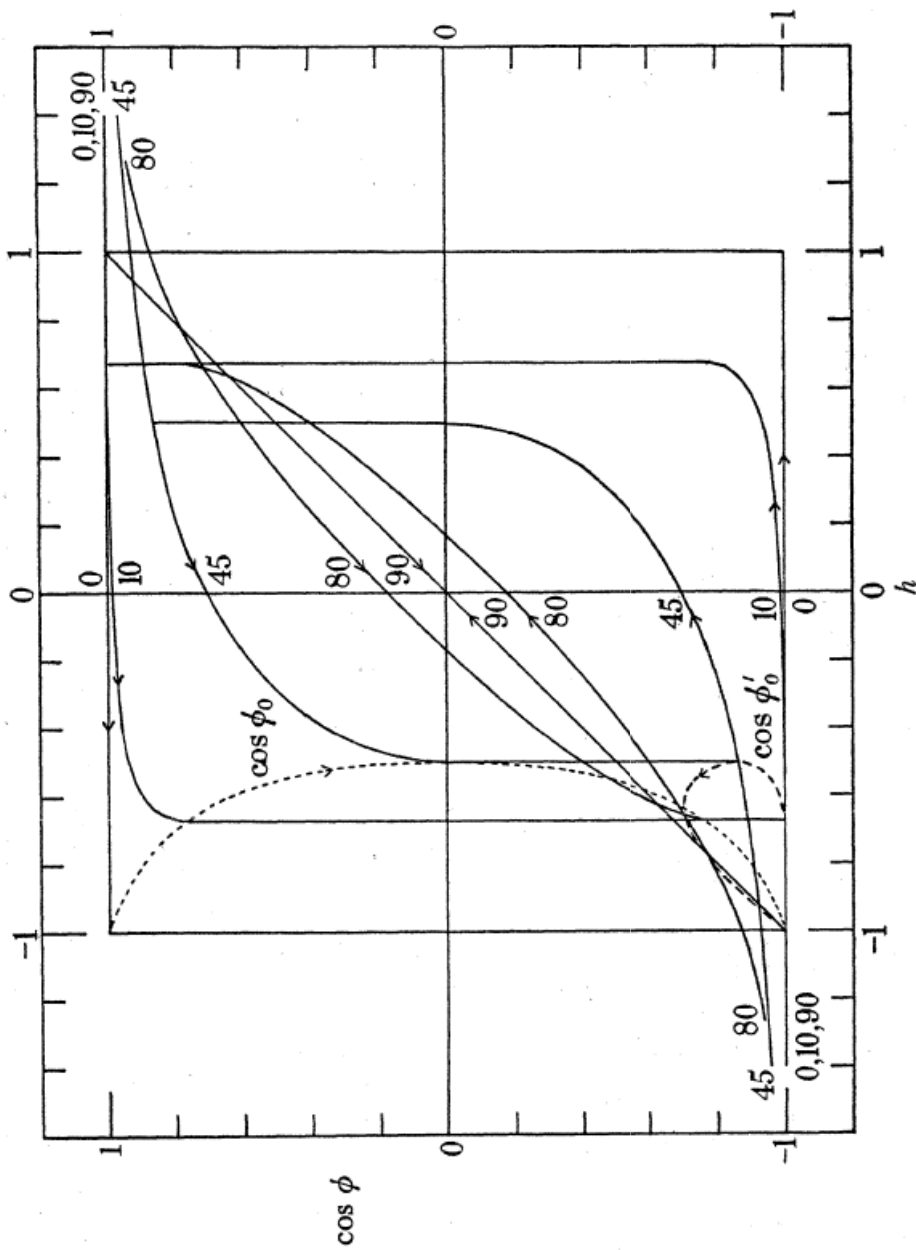


FIGURE 6. Magnetization curves for prolate spheroids. The resolved magnetization in the positive field direction is given by $I_0 \cos \phi$, where I_0 is the saturation magnetization. The field, H , is given by $H = (N_b - N_a) I_0 h$, where N_a and N_b are the demagnetization coefficients along the polar and equatorial axes. The angle, θ , between the polar axis and the direction of the field, is shown, in degrees, by the numbers on the curves. The dotted curves give $\cos \phi_0$ and $\cos \phi'_0$, where ϕ_0 and ϕ'_0 are the angles made with the positive field direction by the magnetization vector at the beginning and end of the discontinuous change at the critical value, h_0 , of the field.

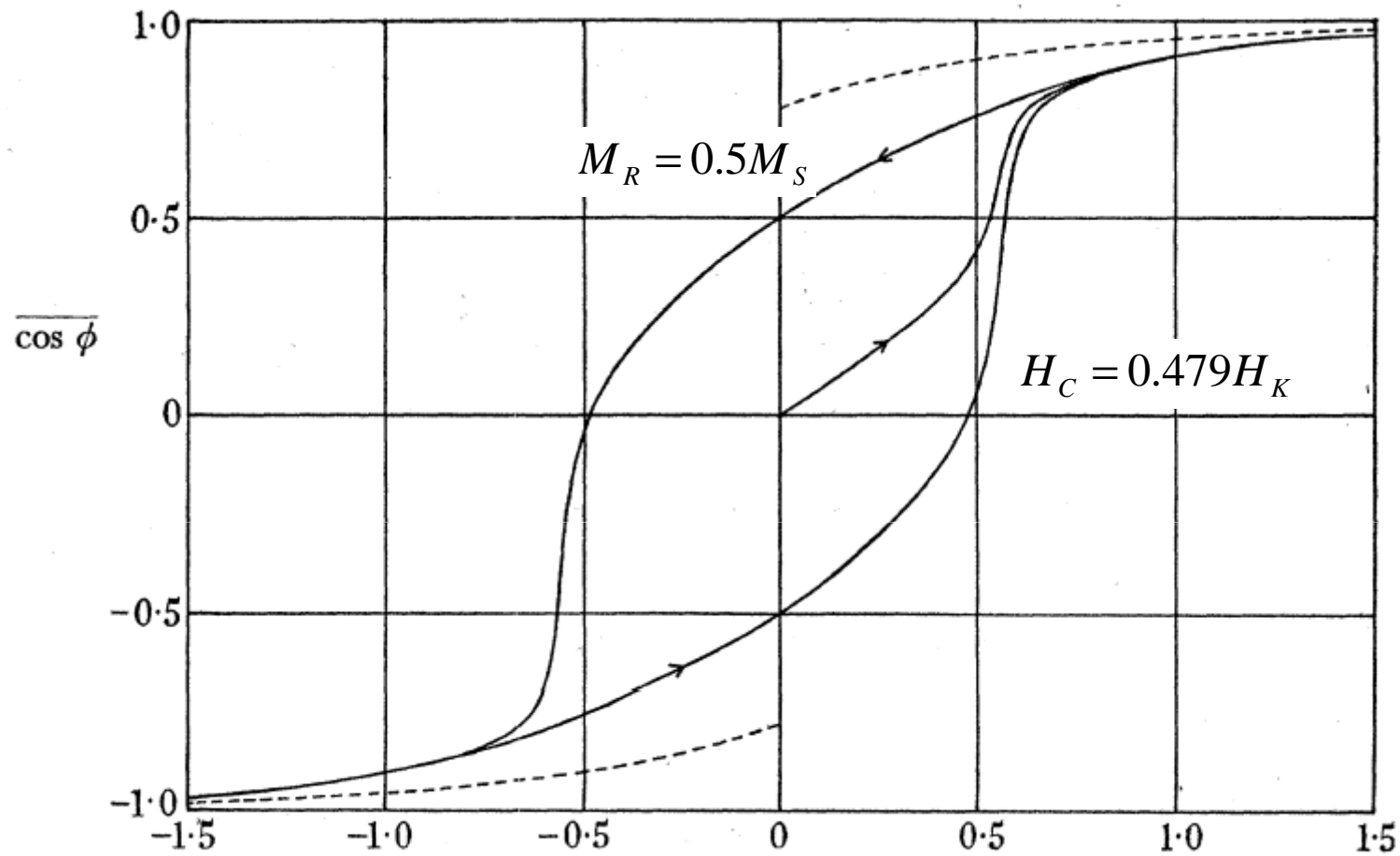


FIGURE 7. Magnetization curves for prolate (full curves) and oblate (broken curves) spheroids orientated at random. The curves refer to similar prolate (or oblate) spheroids orientated at random. $\overline{\cos \phi}$ is proportional to the mean resolved magnetization per spheroid in the positive field direction, or to the resultant magnetization in this direction of the assembly. $H = (|N_a - N_b|) I_0 h$.

Rapid-turnaround characterization methods for MRAM development

by D. W. Abraham,
P. L. Trouilloud,
and D. C. Worledge

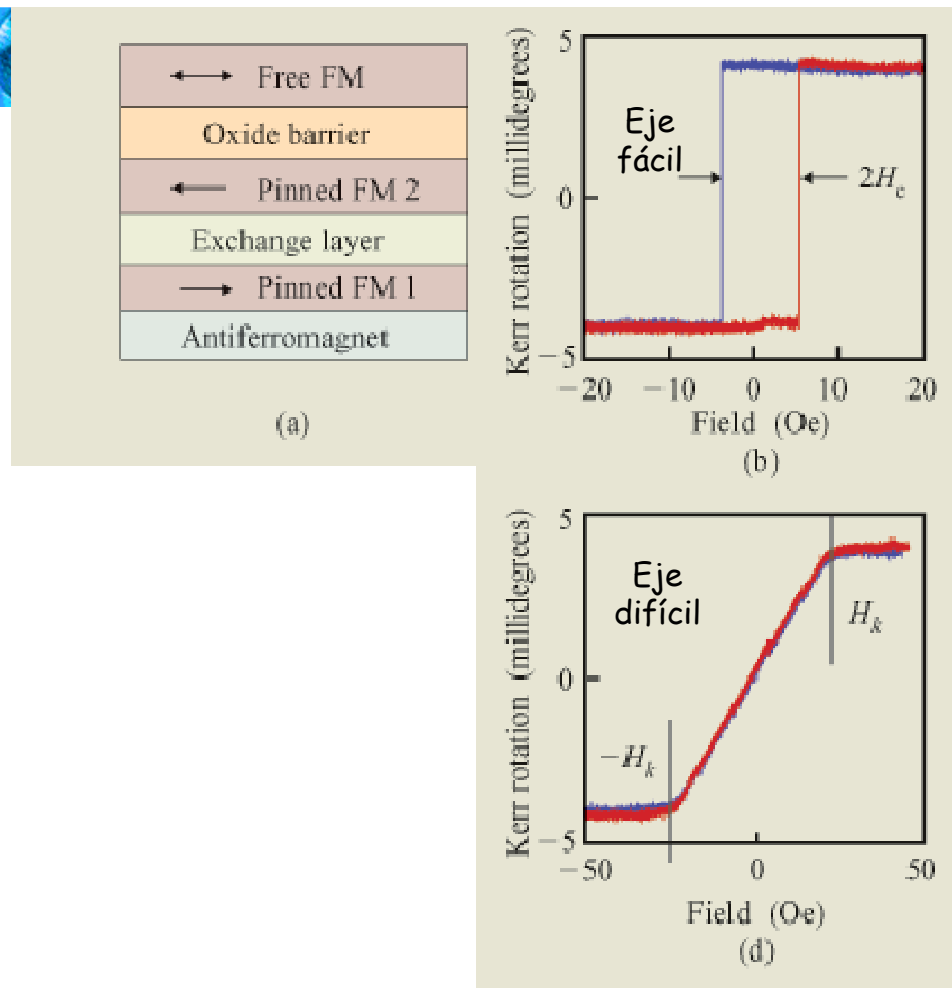
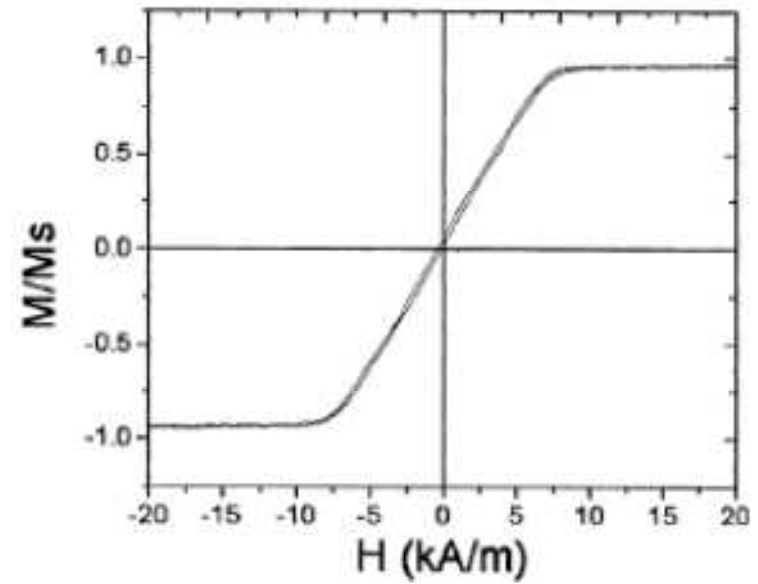
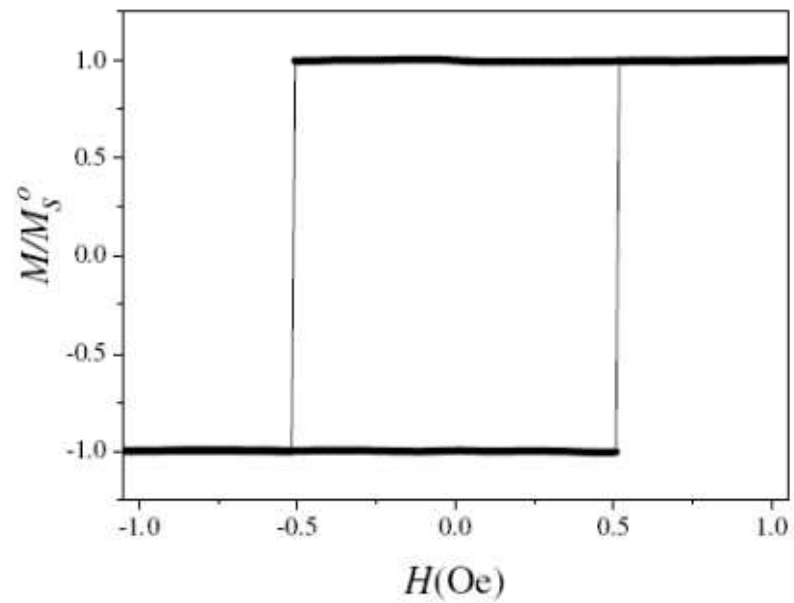
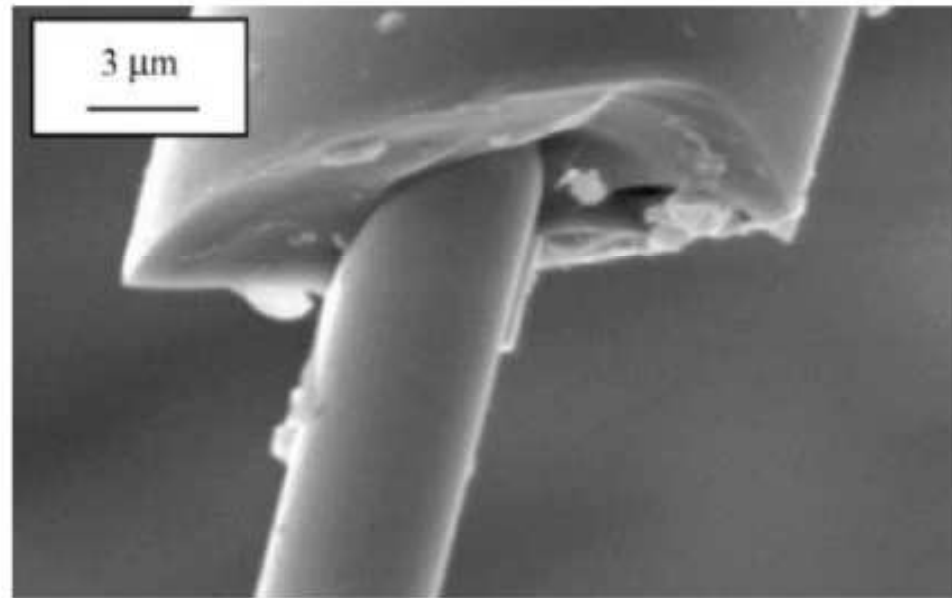


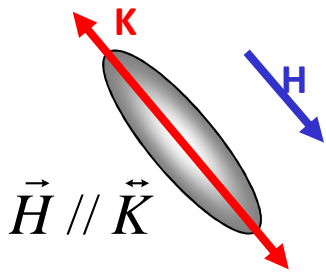
Figure 4

(a) Typical data for a Stoner–Wohlfarth stack. (a) Kerr easy-axis (EA) data taken at low field, showing the excellent low Néel offset and sharp hysteresis loop. (c) High-field EA Kerr magnetometry data showing the relative motion of the magnetization in the two ferromagnetic films, permitting direct measurement of pinning and interlayer coupling. (d) Hard-axis data revealing the film anisotropy.

Microhilos, *P. Mendoza Zéliz et al, 2007*



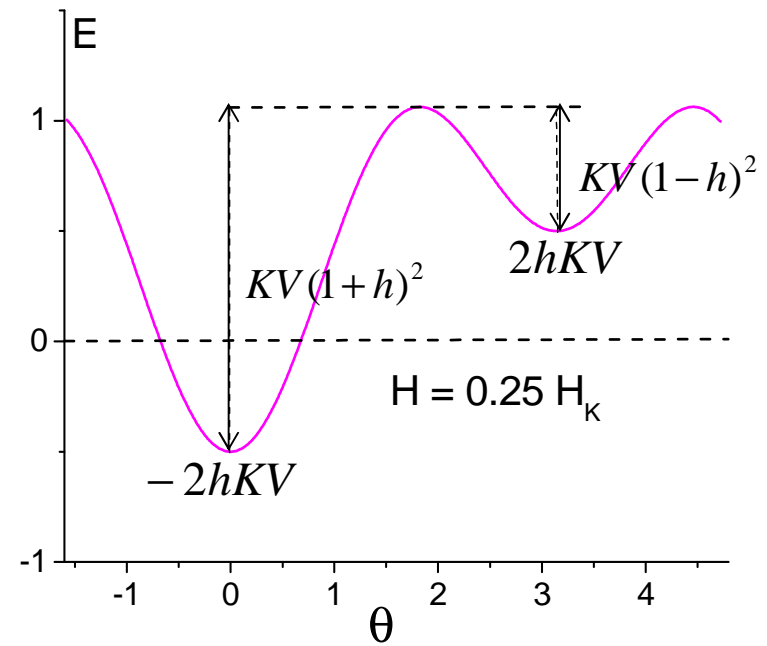
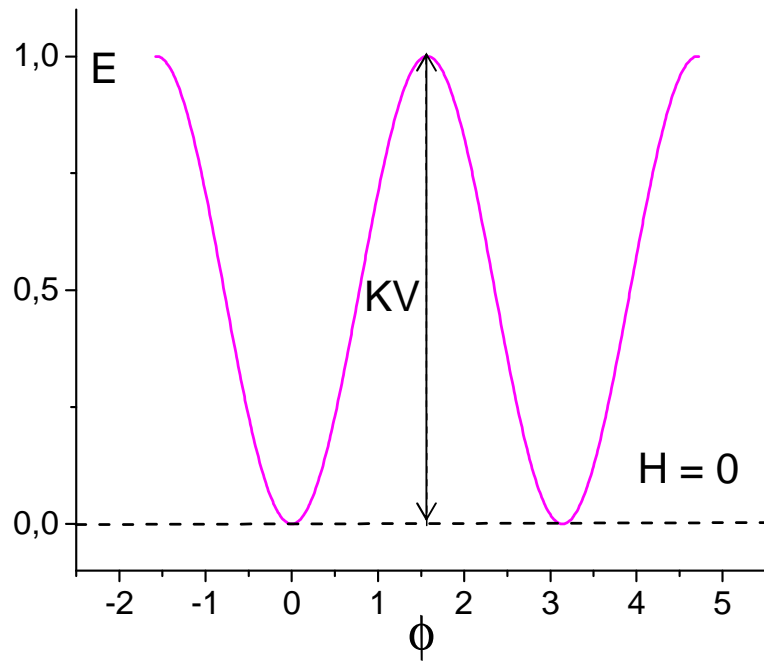
Efectos Dinámicos ($T \neq 0$)

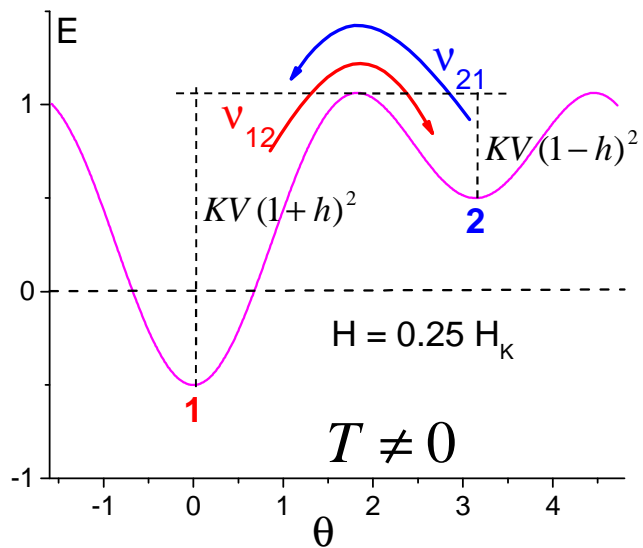


$$E = KV(\sin^2 \phi - 2h \cos \phi)$$

$$h = \frac{H}{H_K}$$

$$H_K = \frac{2K}{\mu_0 M_s}$$





$$\Delta E_{ij} = KV(1+h)^2$$

$$v_{ij} = c_0 e^{-\frac{\Delta E_{ij}}{kT}}$$

Frecuencia de saltos

$$\tau_{ij} = c_0^{-1} e^{\frac{\Delta E_{ij}}{kT}}$$

Tiempo de relajación

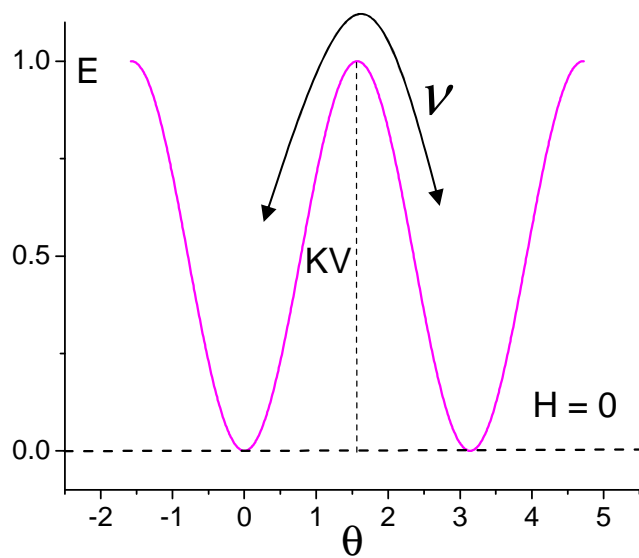
$$\xrightarrow{T=0} v_{ij} = 0$$

$$\xrightarrow{T=\infty} v_{ij} = c_0$$

Frecuencia de intentos

$$\tau_{ij} = c_0^{-1} e^{\frac{\Delta E_{ij}}{kT}}$$

Tiempo de relajación



Para $H = 0$

$$V_{12} = V_{21} = V$$

$$V = V_0 e^{-\frac{KV}{kT}}$$



$$\tau = \tau_0 e^{\frac{KV}{kT}}$$

$$\tau_0 = c_0^{-1}$$

$$10^{-12} \text{ s} \leq \tau_0 \leq 10^{-8} \text{ s}$$

$$\tau = \tau_0 e^{\frac{KV}{kT}}$$

$$\tau_0 \approx cte$$

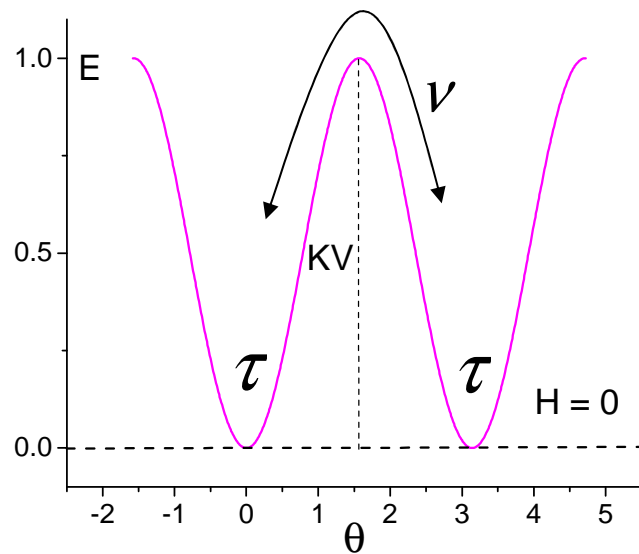
Ejemplo, usando $\tau_0 = 10^{-9}$ s

material	K(J/m ³)	R(nm)	τ (s)
Co	3.9x10 ⁵	4.4	6x10 ⁵
		3.6	0.1
Fe	4.7x10 ⁴	14.0	1.5x10 ⁵
		11.5	0.07

Comportamiento superparamagnético

Tiempo Experimental vs Tiempo de Relajación

$$\tau = \tau_0 e^{\frac{KV}{kT}}$$



Técnica	τ_{exp}
Mössbauer ^{57}Fe , $^{119\text{m}}\text{Sn}$	$\approx 10^{-8}\text{s}$
Susceptibilidad <i>ac</i>	$10^{-4} - 1\text{ s}$
Susceptibilidad <i>ac hf</i>	desde 10^{-6} s
Magnetización <i>dc</i>	$0.1 - 100\text{ s}$

$$\tau_{\text{exp}} < \tau \iff T < T_B$$

Sistema
bloqueado

Patrón estático

Histéresis,
desdoblamiento
Zeeman (EM)

$$\tau_{\text{exp}} > \tau \iff T > T_B$$

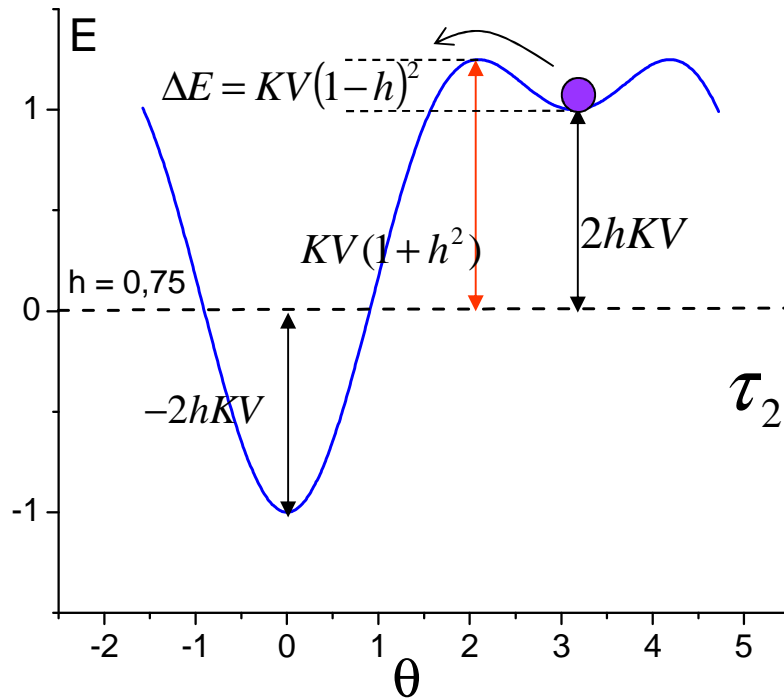
Sistema
desbloqueado

Patrón dinámico

Equilibrio,
patrón super-
paramagnético (EM)

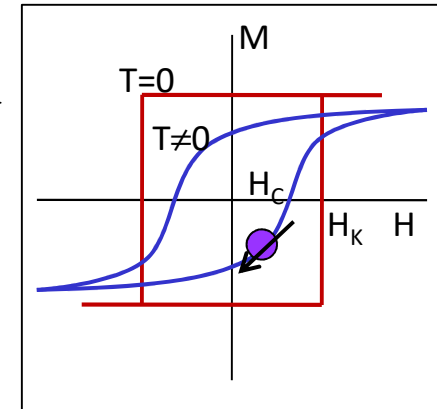
Dependencia del campo coercitivo con la temperatura

$$h = H / H_K = \frac{\mu_0 M_S H}{2K}$$



$$H_C = H_K = \frac{2K}{\mu_0 M_S}$$

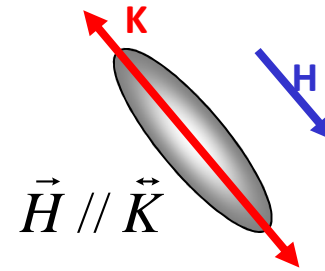
$$\tau_{21} = \tau_0 e^{\frac{KV(1-h)^2}{kT}}$$



a $T \neq 0$ K la inversión de M se producirá cuando $\tau_{21} \approx \tau_{\text{exp}}$

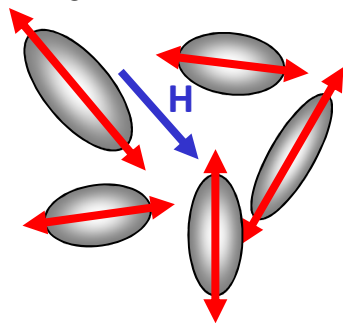
Dependencia del campo coercitivo con la temperatura

$$H_C(T) \approx H_K \left(1 - \sqrt{\frac{kT}{KV} \ln(\tau_{\text{exp}} / \tau_0)} \right)$$

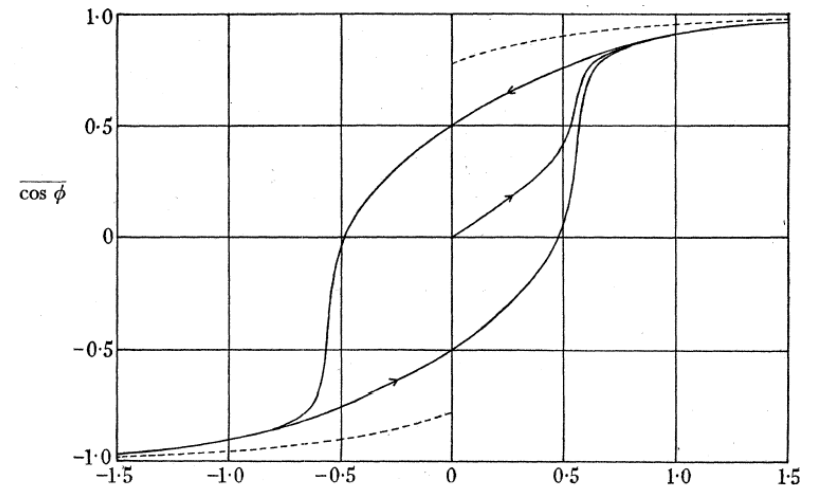


orientación aleatoria

$$H_C(T) \approx 0.48H_K \left(1 - \sqrt{\frac{kT}{KV} \ln(\tau_{\text{exp}} / \tau_0)} \right)$$



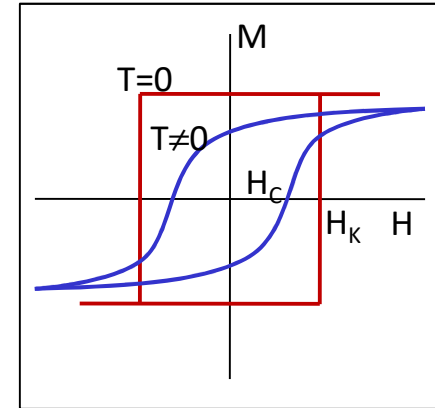
$$H_C(0) = 0.479H_K$$



Temperature Dependent Magnetic Properties of Barium-Ferrite Thin-Film Recording Media

Yingjian Chen, *Member, IEEE*, and Mark H. Kryder, *Fellow, IEEE*

IEEE TRANSACTIONS ON MAGNETICS, VOL. 34, NO. 3, MAY 1998



$$H_c(T) \approx cH_K \left(1 - \left[\frac{kT}{KV} \ln(\tau_{\text{exp}} / \tau_0) \right]^n \right)$$

$c = 1$

introduciendo

$$T_B = \frac{KV}{k \ln(\tau_{\text{exp}} / \tau_0)}$$

the easy axis orientation. In a system with uniaxially aligned easy axes, τ is $1/2$ [29], and in a system with random easy axis orientations, τ is $2/3$ [30]. The fitting parameters V_{sw}

[29] M. P. Sharrock and J. T. McKinney, *IEEE Trans. Magn.*, vol. MAG-17, p. 3020, 1981.

[30] R. H. Victora, "Predicted time dependence of the switching field for magnetic materials," *Phys. Rev. Lett.*, vol. 63, pp. 457-460, 1989.

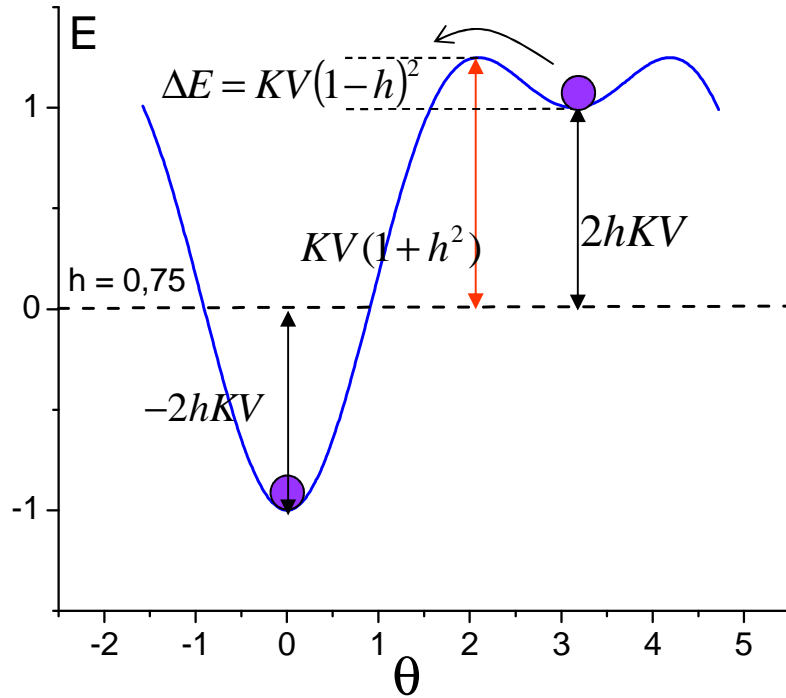
$c = 0.48$

$$H_c = c \frac{2K}{\mu_0 M_s} \left[1 - \left(\frac{T}{T_B} \right)^{1/2} \right]$$

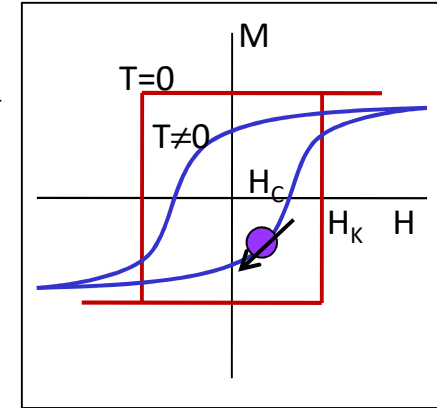
expresión de uso extendido

Dependencia del campo coercitivo con la temperatura 2

$$h = H / H_K = \frac{\mu_0 M_S H}{2K}$$



$$H_C = H_K = \frac{2K}{\mu_0 M_S}$$



a $T \neq 0$ K la inversión de M se producirá cuando $\tau_{21} \approx \tau_{\text{exp}}$

$$\tau_{12} = \tau_0 e^{\frac{KV(1+h)^2}{kT}} \quad f_{12} = \nu_0 e^{-\frac{KV(1+h)^2}{kT}}$$

$$\tau_{21} = \tau_0 e^{\frac{KV(1-h)^2}{kT}} \quad f_{21} = \nu_0 e^{-\frac{KV(1-h)^2}{kT}}$$

Población de los estados orientacionales

$$P_1 + P_2 = 1$$

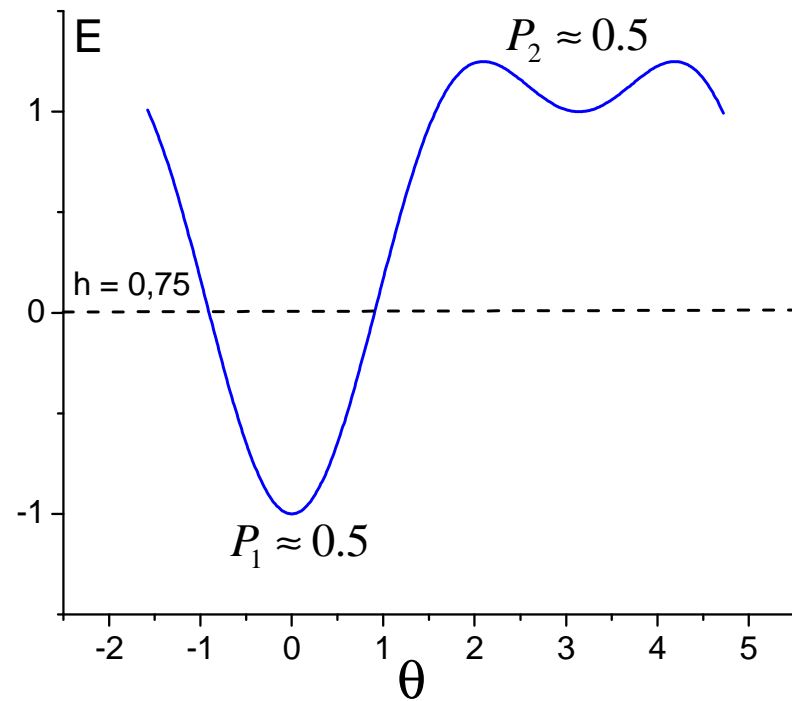
$$M \approx 0 \rightarrow P_1 \approx P_2 \approx 0.5$$

Evolución temporal

Por el principio del balance detallado

$$\frac{dP_1}{dt} = P_2 f_{21} - P_1 f_{12}$$

$$\frac{dP_1}{dt} \approx 0.5(f_{21} - f_{12})$$



$$M = M_s(P_1 - P_2) = M_s(2P_1 - 1)$$

$$\frac{dM}{dt} = 2M_s \frac{dP_1}{dt} \approx M_s(f_{21} - f_{12})$$

$$\frac{1}{\nu_0 M_s} \frac{dM}{dt} \approx e^{-\frac{KV(1-h)^2}{kT}} - e^{-\frac{KV(1+h)^2}{kT}}$$

$$\frac{1}{v_0 M_S} \frac{dM}{dt} \approx e^{-\frac{KV(1-h)^2}{kT}} - e^{-\frac{KV(1+h)^2}{kT}} \approx e^{-\frac{KV(1-h)^2}{kT}}$$

$$\frac{1}{v_0 M_S} \frac{dM}{dt} \approx e^{-\frac{KV(1-h)^2}{kT}} - e^{-\frac{KV(1+h)^2}{kT}} \approx e^{-\frac{KV(1-h)^2}{kT}}$$

$$\frac{dM}{dt} = \frac{dM}{dH} \frac{dH}{dt}$$

cuando $H \approx H_C \rightarrow \frac{dM}{dH} = \chi \approx cte$

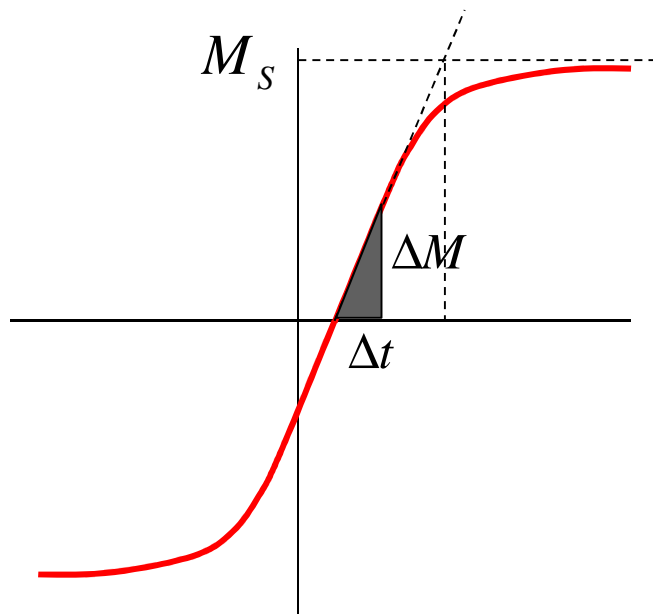
$$\left. \frac{1}{v_0 M_S} \chi \frac{dH}{dt} \right|_{H_C} \approx e^{-\frac{KV(1-h_C)^2}{kT}}$$

$$H_C \approx H_K \left\{ 1 - \sqrt{\frac{kT}{KV} \ln \left[\frac{M_S}{\chi (dH/dt)_{H_C}} \frac{1}{\tau_0} \right]} \right\}$$

$$\tau_0 = 1/c_0$$

escribiendo $\chi \approx \Delta M / \Delta H$, $dH / dt \approx \Delta H / \Delta t$

$$H_C \approx H_K \left\{ 1 - \sqrt{\frac{kT}{KV} \ln \left[\frac{(M_S / \Delta M) \Delta t}{\tau_0} \right]} \right\}$$



llamando $n = M_S / \Delta M$ $\tau_{\text{exp}} = n \Delta t$

$$H_C \approx H_K \left\{ 1 - \sqrt{\frac{kT}{KV} \ln \left(\frac{\tau_{\text{exp}}}{\tau_0} \right)} \right\}$$

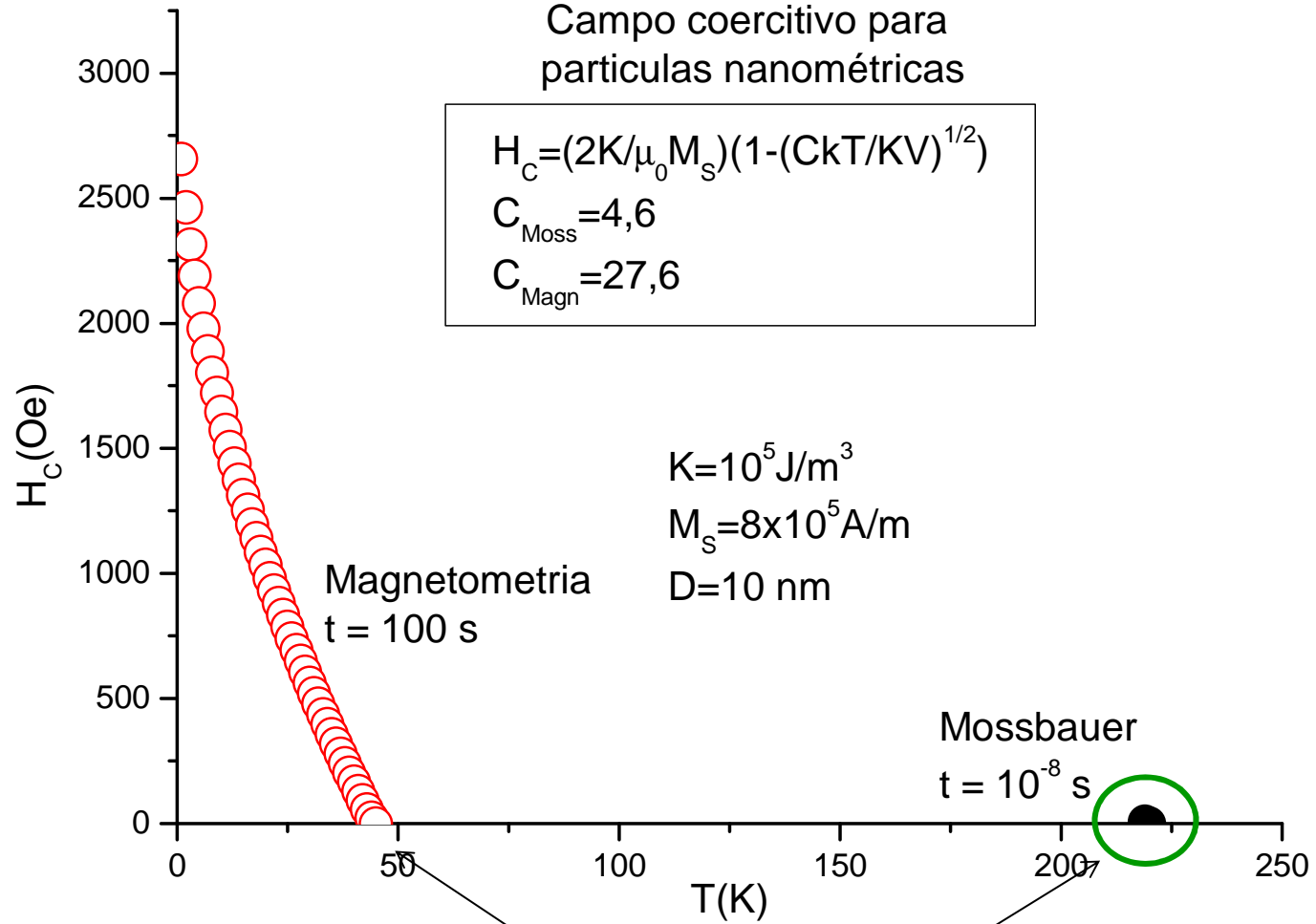
Donde τ_{exp} sería el tiempo aproximado requerido para alcanzar la saturación desde $M = 0$

Campo coercitivo para
partículas nanométricas

$$H_C = (2K/\mu_0 M_S) (1 - (CkT/KV)^{1/2})$$

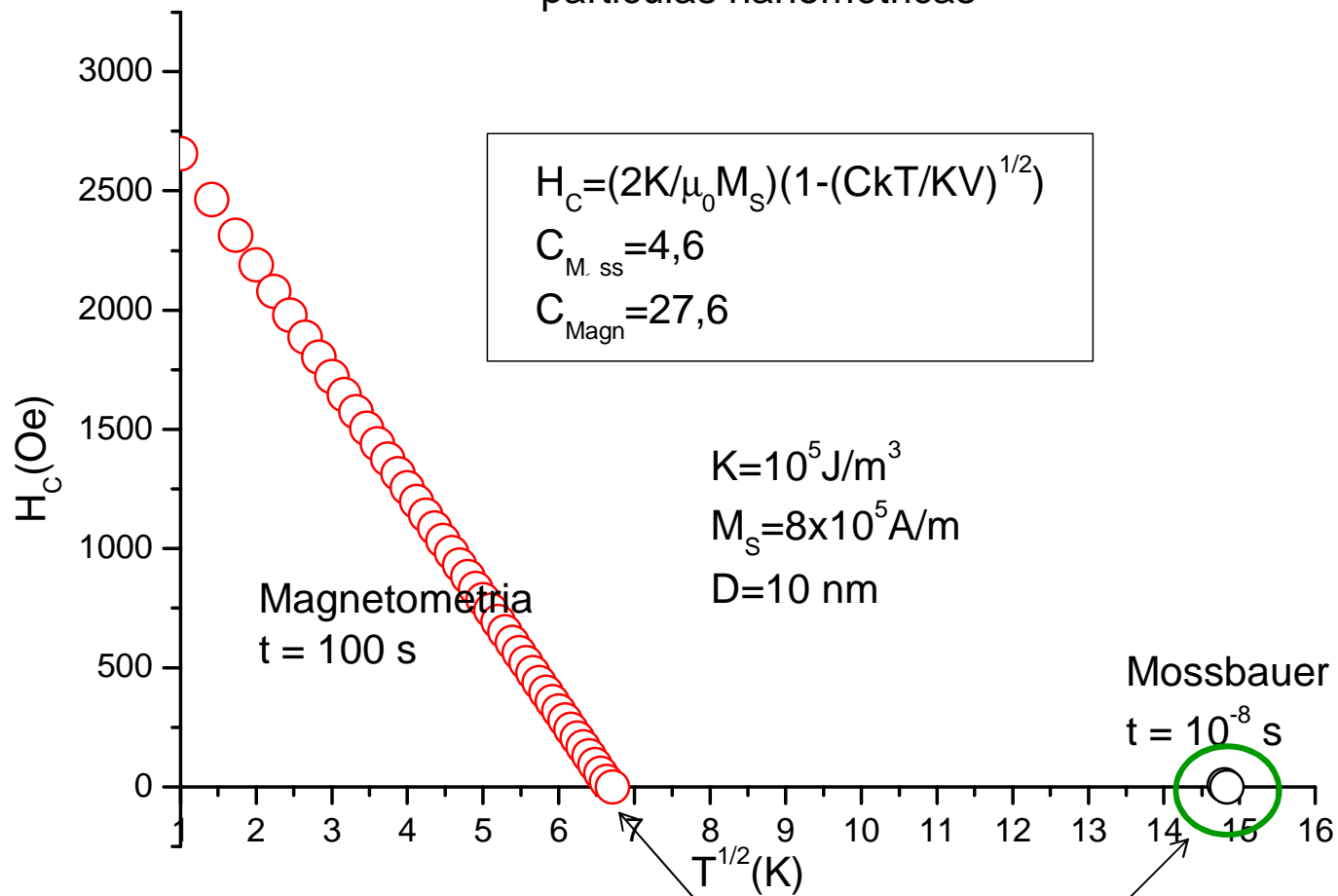
$$C_{\text{Moss}} = 4,6$$

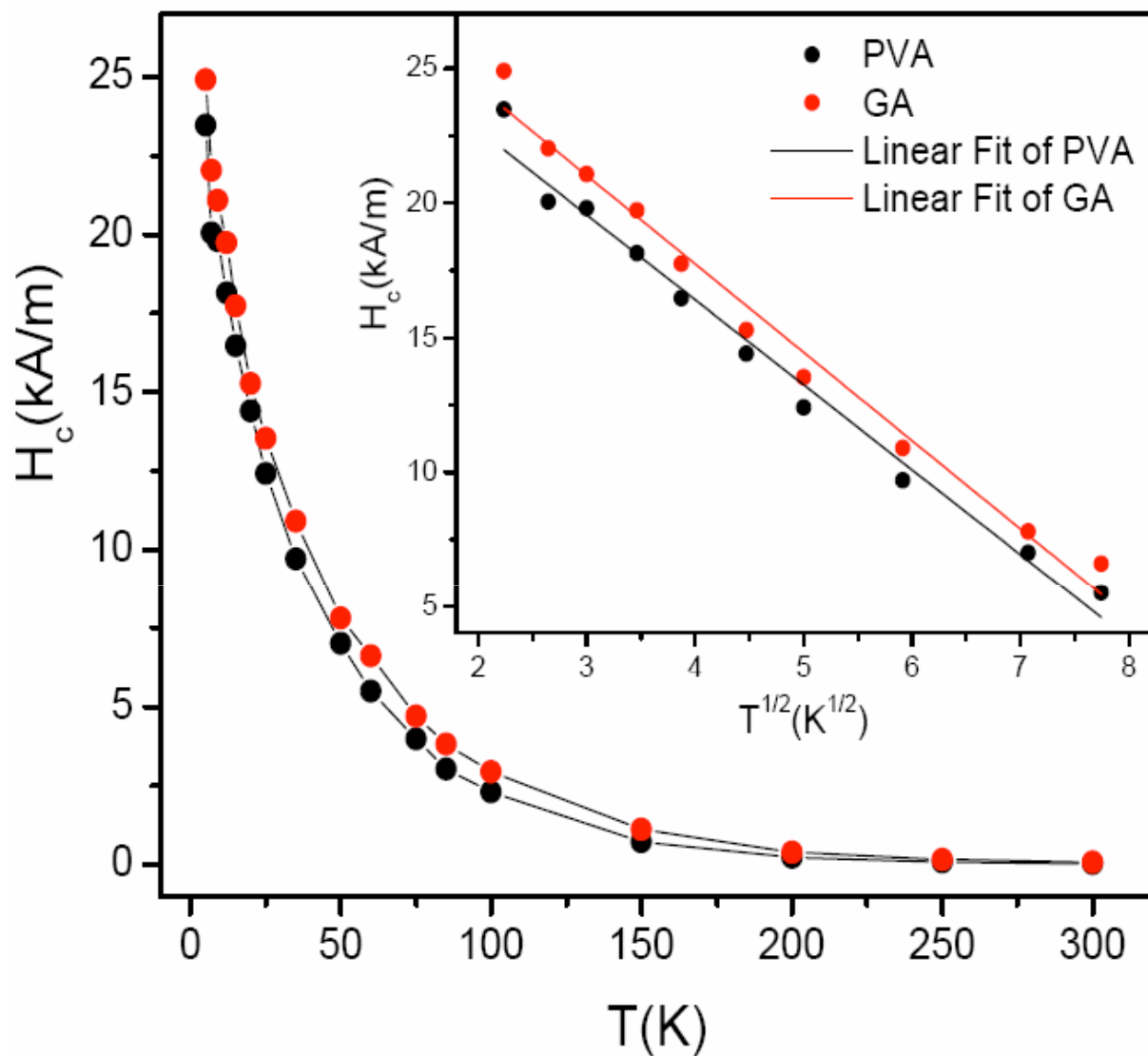
$$C_{\text{Magn}} = 27,6$$



$$T = T_B$$

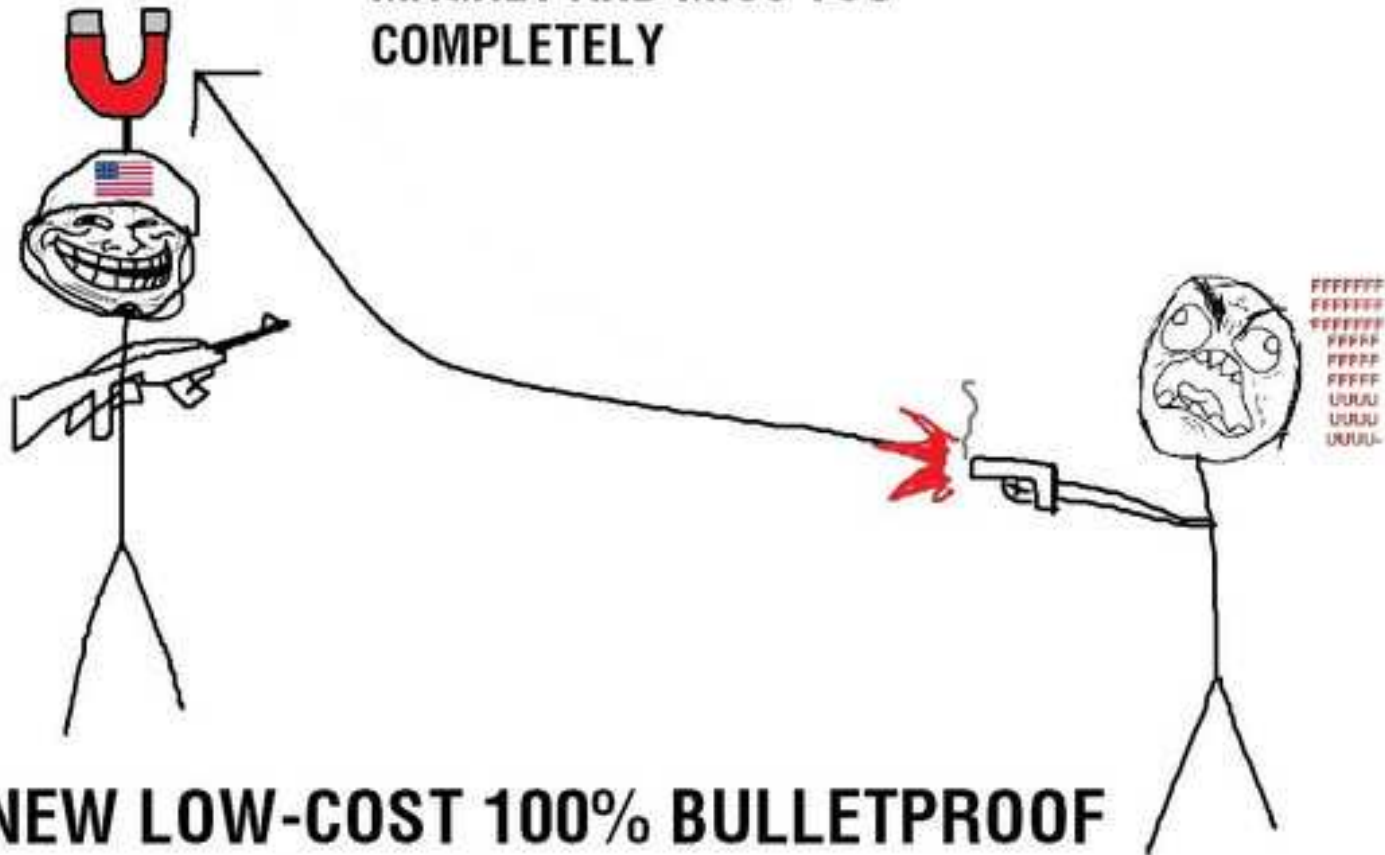
Campo coercitivo para
partículas nanométricas





Ferrogel de NP de magnetita (8 nm) en hidrogel de PVA, Mendoza Zélis et al, enviado

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